

Interactions in regression

Binary Variable Interactions

Outcome = Systolic BP

No interaction

	Drink = 0	Drink = 1
Smoke = 1	a	a + b
Smoke = 0	0	b

a = Smoking effect, b = Drinking effect

Binary Variable Interactions

Outcome = Systolic BP

Interaction

	Drink = 0	Drink = 1
Smoke = 1	a	a + b + c
Smoke = 0	0	b

$c \neq 0$

a = Smoking effect, b = Drinking effect, c = interaction

Binary Variable Interaction with a Continuous Variable

$$y = \alpha + x_{age}\beta_{age} + x_{Dx}\beta_{Dx} + x_{age}x_{diag}\beta_{inter} + \varepsilon$$

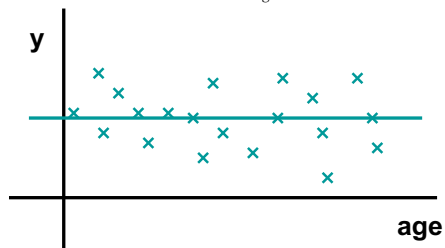
y = cognition score - outcome

$Dx = 1$, AD (Alzheimer's)

$Dx = 0$, HC (Healthy Control)

Case 1

$$\beta_{age} = 0, \beta_{Dx} = 0, \beta_{inter} = 0$$



$$y = \alpha + x_{age}\beta_{age} + x_{Dx}\beta_{Dx} + x_{age}x_{diag}\beta_{inter} + \varepsilon$$

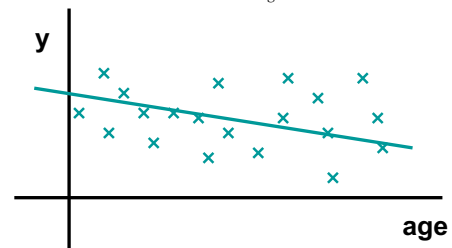
y = cognition score - outcome

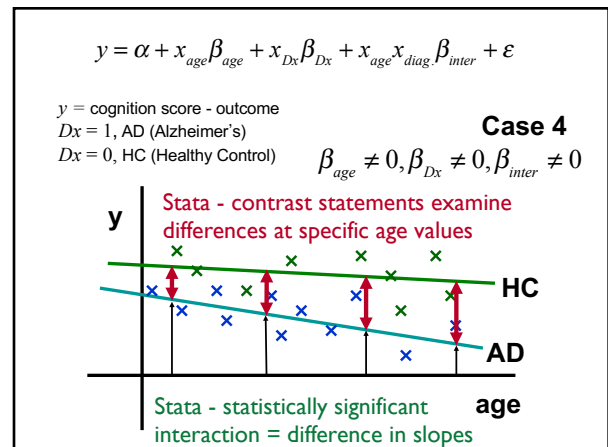
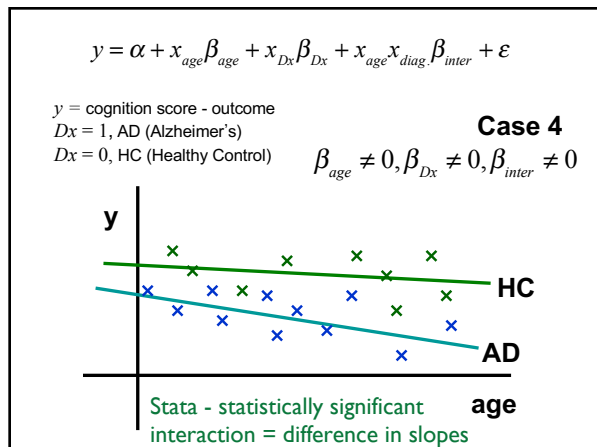
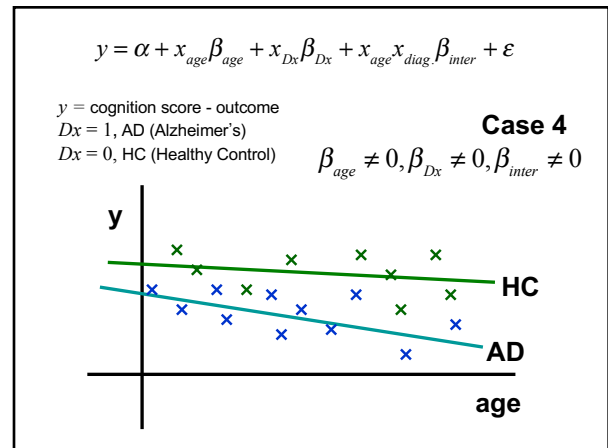
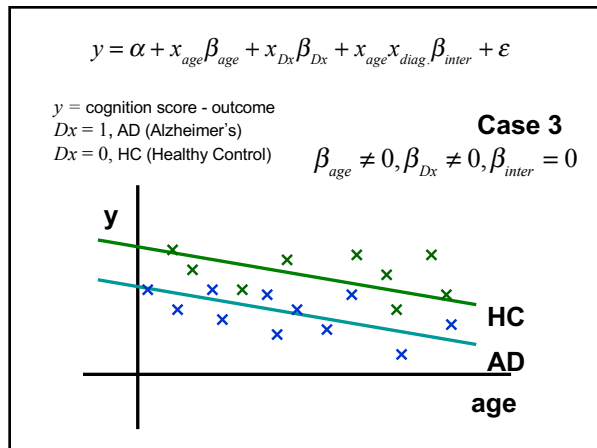
$Dx = 1$, AD (Alzheimer's)

$Dx = 0$, HC (Healthy Control)

Case 2

$$\beta_{age} \neq 0, \beta_{Dx} = 0, \beta_{inter} = 0$$





Note: continuous variable by continuous variable interaction even trickier to interpret – we won't go there