

Sample size Calculations

- Sample size calculations using Stata
- Tests for categorical data

Sample size calculations

- Set significance level, α , and the desired power (80-90%)
- Specify your hypothesized mean value for each group
- Estimate the sample standard deviation for each group

Sample size calculations

- Example: We will conduct an intervention that we think will increase CD4 count among HIV-infected persons. We will randomize a control versus the intervention, and we think it will increase CD4 count from 350 to 450. The SD for CD4 count for our previous studies was 250.

Sample size Calculations

```
. power twomeans 350 450, sd(250)
```

```
Performing iteration ...
```

```
Estimated sample sizes for a two-sample means test
```

```
t test assuming sd1 = sd2 = sd
```

```
Ho: m2 = m1 versus Ha: m2 != m1
```

```
Study parameters:
```

```
alpha = 0.0500
```

```
power = 0.8000
```

```
delta = 100.0000
```

```
m1 = 350.0000
```

```
m2 = 450.0000
```

```
sd = 250.0000
```

```
Estimated sample sizes:
```

```
N = 200
```

```
N per group = 100
```

Sample size Calculations

We write this up as:

With a sample of size 200 (100 in each group), we will have 80% power to detect a difference of 100 or greater in CD4 cell count if the CD4 cell count in the control group is 350 and the standard deviation in both groups is 250, at significance level=0.05.

- Writing sample size statements: <https://www-users.york.ac.uk/~mb55/guide/size.htm>

Other sample size calculators:

- UCSF online <http://www.sample-size.net/>
- Other online calculators (try <http://powerandsamplesize.com/Calculators/>)

Statistical hypothesis tests

Data and comparison type	Alternative hypotheses	Parametric test Stata command	Non-parametric test Stata command
Numerical; One mean	$H_a: \mu \neq \mu_a$ (two-sided) $H_a: \mu > \mu_a$ or $\mu < \mu_a$ (one-sided)	Z or t-test • <code>ttest var1=hypoth val.*</code>	
Numerical; Two means, <u>paired data</u>	$H_a: \mu_1 \neq \mu_2$ (two-sided) $H_a: \mu_1 > \mu_2$ or $\mu < \mu_a$ (one-sided)	Paired t-test • <code>ttest var1=var2*</code>	Sign test • <code>signtest var1=var2</code> • Wilcoxon Signed-Rank <code>signrank var1=var2</code>)
Numerical; Two means, independent data	$H_a: \mu_1 \neq \mu_2$ (two-sided) $H_a: \mu_1 > \mu_2$ or $\mu < \mu_a$ (one-sided)	T-test (equal or unequal variance) • <code>ttest var1, by(byvar) unequal</code>	Wilcoxon rank-sum test • <code>ranksum var1, by(byvar)</code>
Numerical, Two or more means, independent data	$H_a: \mu_1 \neq \mu_2$ or $\mu_1 \neq \mu_3$ or $\mu_2 \neq \mu_3$ etc.	ANOVA • <code>oneway var1 byvar</code>	Kruskal Wallis test • <code>kwallis var1, by(byvar)</code>
Dichotomous; One proportion	$H_a: p \neq p_a$ (two-sided) $H_a: p > p_a$ or $p < p_a$ (one-sided)	Proportion test • <code>prtest var1=hypoth value*</code> • <code>bitest var1=hypoth value</code>	
Dichotomous; two proportions	$H_a: p_1 \neq p_2$ (two-sided) $H_a: p_1 > p_2$ (one-sided)	Proportion test (z-test) • <code>prtest var1, by(byvar)</code>	Chi-square test • <code>tab var1 var2, chi exact</code> McNemar's for paired data: • <code>mcc var1 var2</code>
Categorical by categorical (nxk)	H_a : The rows not independent of the columns		Chi-square test • <code>tab var1 var2, chi exact</code>

Categorical outcomes

- With the exception of the proportion test, all the previous tests were for comparing numerical outcomes and categorical variables (e.g. predictors)
 - e.g., CD4 count by alcohol consumption
- We often have dichotomous outcomes and variates
 - e.g. Having any children by sex

Categorical outcomes

- We can make tables of the number of observations falling into each category
- These are called contingency tables
- e.g. Currently having any children by sex

```
. tab children_any gender
```

children_a			
ny - Do			
you have gender - What is your			
any gender?			
children?	Male	Female	Total
-----+-----+-----+-----			
0	24	23	47
1	2	6	8
-----+-----+-----+-----			
Total	26	29	55

Contingency tables

- Often summaries of counts of disease versus no disease and exposed versus not exposed
- Frequently 2x2 but can generalize to $n \times k$
 - n rows, k columns
- Note that Stata sorts on the numeric value, so for 0-1 variables the disease state will be the 2nd row

		Exposure		Total
		+	-	
Disease	+	a	b	a+b
	-	c	d	c+d
Total		a+c	b+d	n=a+b+c+d

Contingency tables

- Contingency tables are usually summaries of data that originally looked like this.

Example of data set		
Obs.	Exposure (1=yes; 0=no)	Disease (1=yes; 0=no)
1	1	1
2	1	0
3	1	1
4	0	0
5	1	1
6	1	0
7	0	0
...	...	...
n	0	0

Categorical outcomes

- Say we want to know whether the proportion with children varies by gender in biostats classes
- We could test the null hypothesis that the proportion of males with children equals that of females.
- $H_0: p_{w/\text{children males}} = p_{w/\text{children females}}$
- $H_A: p_{w/\text{children males}} \neq p_{w/\text{children females}}$
- This is the test of proportions from Lecture 6

Recall: The Proportion test

```
. . prtest children_any, by(gender)
```

Two-sample test of proportions

Male: Number of obs = 26
Female: Number of obs = 29

Variable	Mean	Std. Err.	z	P> z	[95% Conf. Interval]
Male	.0769231	.0522589			-.0255026 .1793487
Female	.2068966	.0752216			.0594649 .3543282
diff	-.1299735	.091593			-.3094925 .0495456
under Ho:	.0952197	-1.36	0.172		

diff = prop(Male) - prop(Female) z = -1.3650
Ho: diff = 0

Ha: diff < 0
Pr(Z < z) = 0.0861

Ha: diff != 0
Pr(|Z| > |z|) = 0.1723

Ha: diff > 0
Pr(Z > z) = 0.9139

Categorical outcomes

- There are other methods to do this (chi-square test)
- Why?
 - These methods are more general – can be used when you have more than 2 levels in either variable
- We will start with the 2x2 example however

Categorical outcomes

- Overall, the probability of having any children overall in this sample is $8/55=0.1455$ This is the marginal probability of having children (in this class)
- There were 26 males and 29 females
- Under the null hypothesis, the expected proportion in each group is the overall proportion
- So the expected number of students who have children:

Males $26 * .1455 = 3.8$

Females: $29 * .1455 = 4.2$

Categorical outcomes

- We can also calculate the expected number without children under the null hypothesis of no difference
 - Males: $26 \times (1 - .1455) = 22.2$
 - Females: $29 \times (1 - .1455) = 24.8$
- Observed & Expected counts

Observed data

```
. tab children_any gender
```

children_a				
ny - Do				
you have	gender - What is your			
any	gender?			
children?	Male	Female		Total
0	24	23		47
1	2	6		8
Total	26	29		55

EXPECTED COUNTS UNDER THE NULL HYPOTHESIS

```
. tab children_any gender, expected nof
```

children_a				
ny - Do				
you have	gender - What is your			
any	gender?			
children?	Male	Female		Total
-----+-----+-----				
0	22.2	24.8		47.0
1	3.8	4.2		8.0
-----+-----+-----				
Total	26.0	29.0		55.0

Categorical outcomes

- Generically

Expected counts		Exposure		Total
		+	-	
Disease	+	$(a+b)(a+c)/n$	$(a+b)(b+d)/n$	a+b
	-	$(c+d)(a+c)/n$	$(c+d)(b+d)/n$	c+d
Total		a+c	b+d	n=a+b+c+d

Categorical outcomes

- The Chi-squared test compares the observed frequency (O) in each cell with the expected frequency (E) under the null hypothesis of no difference
- The differences $O-E$ are squared, divided by E , and added up over all the cells
- The sum of this is the test statistic and follows a chi-square distribution

Chi-squared test of independence

- The chi-squared test statistic (for the test of independence in contingency tables) for a 2x2 table (dichotomous outcome, dichotomous exposure)

$$X_1^2 = \sum_{i=1}^4 \left(\frac{(O_i - E_i)^2}{E_i} \right)$$

- i is the index for the cells in the table – there are 4 cells
- This test statistic is compared to the chi-squared distribution with 1 degree of freedom

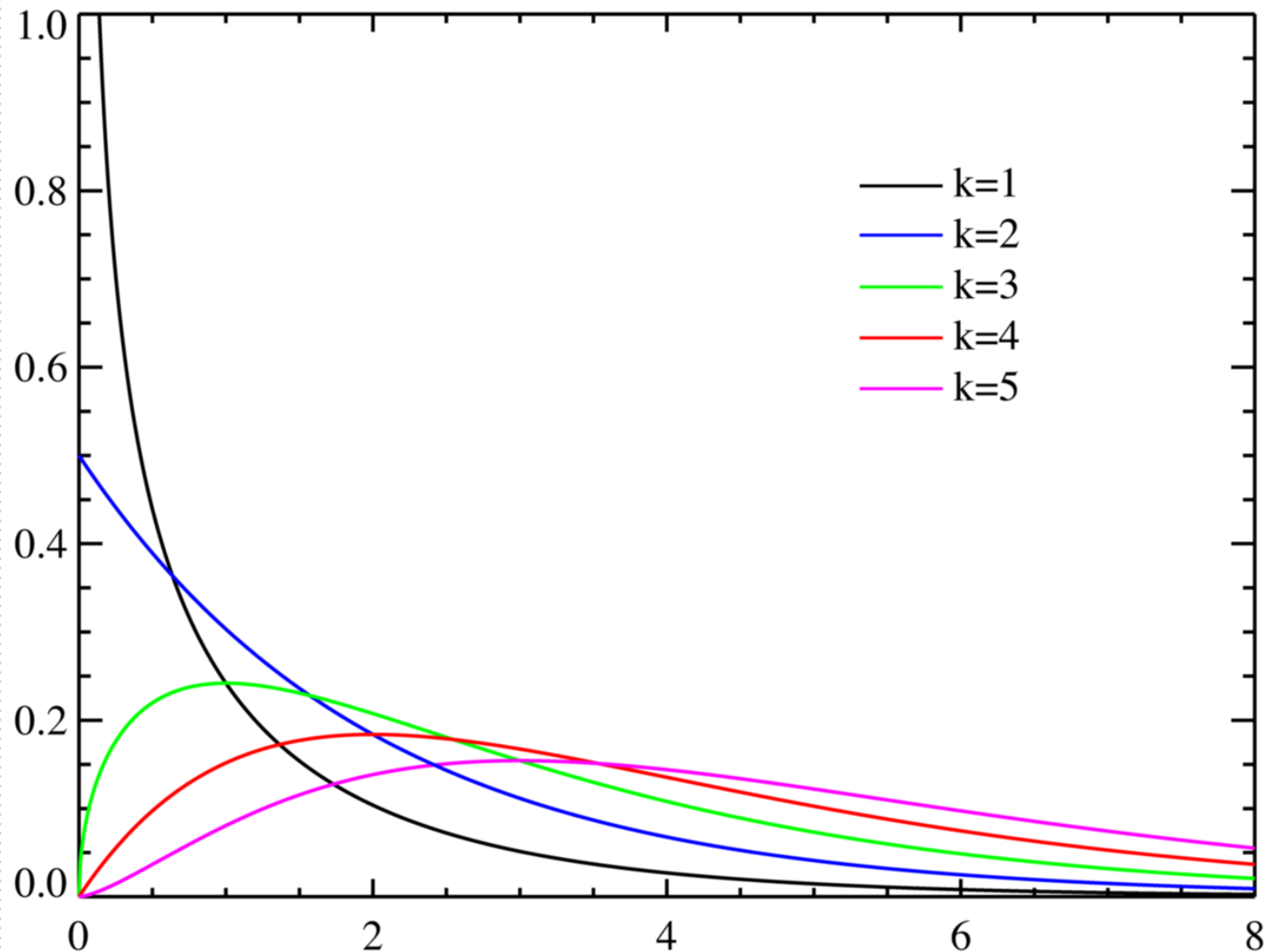
Chi-squared test of independence

- The chi-square test statistic for the test of independence in an $n \times k$ contingency table is

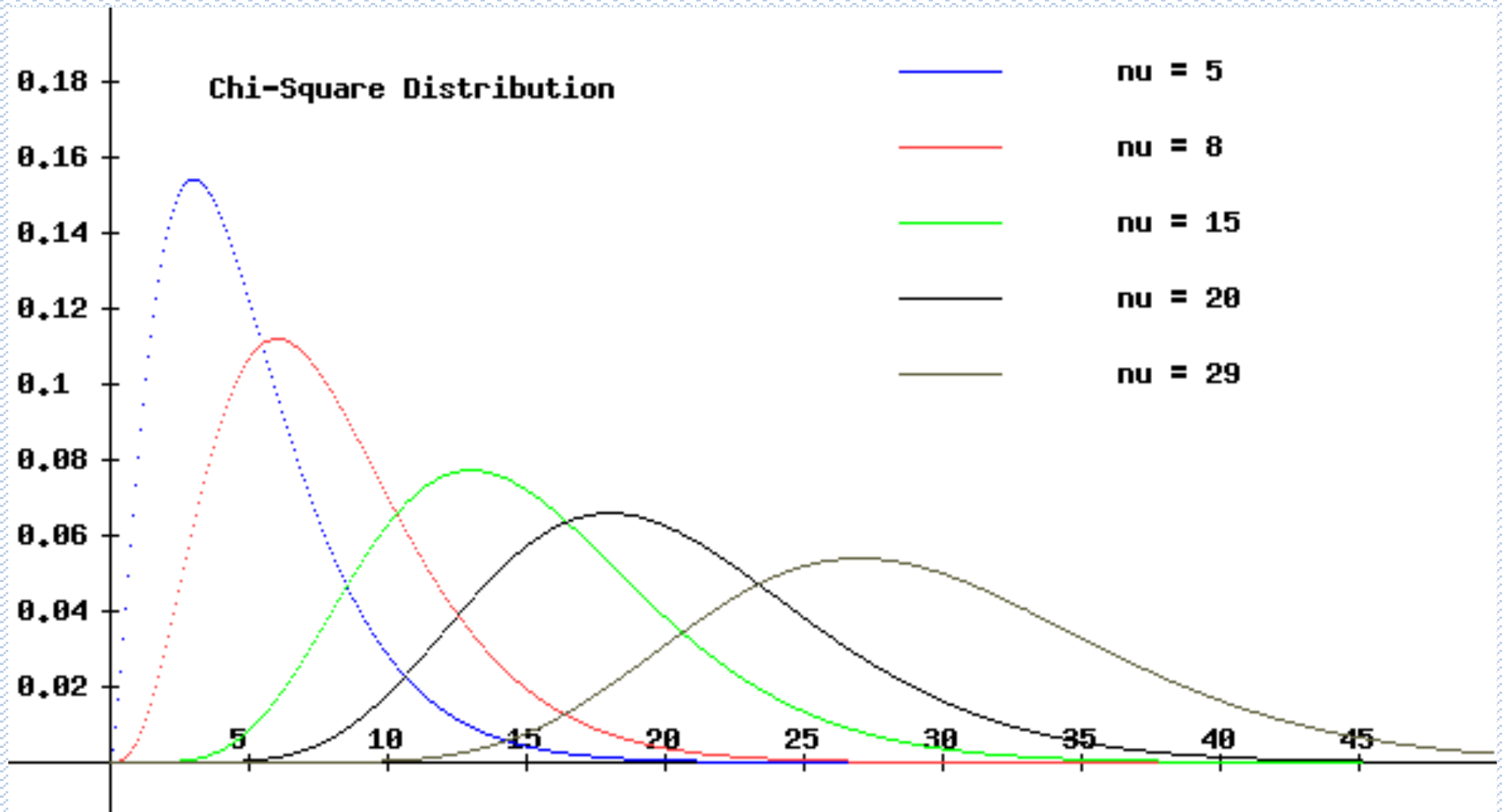
$$X^2_{(n-1)*(k-1)} = \sum_{i=1}^{nk} \left(\frac{(O_i - E_i)^2}{E_i} \right)$$

- This test statistic is compared to the chi-squared distribution
- The degrees of freedom for this test are $(n-1)*(k-1)$, so for a 2×2 there is 1 degree of freedom
 - n =the number of rows; k =the number of columns in the $n \times k$ table
 - The chi-squared distribution with 1 degree of freedom is actually the square of a standard normal distribution
- Expected cell sizes should all be >1 and fewer than 20% should be <5
- The Chi-squared test is for two sided hypotheses

Chi-squared distribution



Chi-squared distribution



Mean = degrees of freedom
Variance = $2 \times \text{degrees of freedom}$

Chi-squared test of independence

- For the example, the chi-squared statistic for our 2x2 is
- $$di = (24-22.2)^2/22.2 + (23-24.8)^2/24.8 + (2-3.8)^2/3.8 + (6-4.2)^2/4.2$$
- 1.9006513

There is 1 degree of freedom

- Probability of observing a chi-squared value of 0.0309 with 1 degree of freedom

```
. di chi2tail(1,1.901)  
. .16796643
```

Fail to reject the null hypothesis of
independence

Categorical outcomes

```
. . tab children_any gender, chi
```

```
children_a |  
  ny - Do |  
  you have | gender - What is your  
    any |      gender?  
children? |      Male      Female |      Total  
-----+-----+-----  
      0 |      24      23 |      47  
      1 |       2       6 |       8  
-----+-----+-----  
    Total |      26      29 |      55
```

Pearson chi2(1) = 1.8632 Pr = 0.172

Test statistic (df)

p-value

If you want to see the row or column percentages, use row or col options

```
tab children_any gender, row col chi expected
```

```
+-----+
| Key      |
+-----+
| frequency |
| expected frequency |
| row percentage |
| column percentage |
+-----+
```

children_a			
ny - Do			
you have	gender - What is your		
any	gender?		
children?	Male	Female	Total
0	24	23	47
	22.2	24.8	47.0
	51.06	48.94	100.00
	92.31	79.31	85.45
1	2	6	8
	3.8	4.2	8.0
	25.00	75.00	100.00
	7.69	20.69	14.55
Total	26	29	55
	26.0	29.0	55.0
	47.27	52.73	100.00
	100.00	100.00	100.00

```
Pearson chi2(1) = 1.8632 Pr = 0.172
```

Test of independence

- For small cell sizes in 2x2 tables, use the Fisher exact test
- It is based on a discrete distribution called the hypergeometric distribution
- For 2x2 tables, you can choose a one-sided (results as or more extreme only in one direction) or a two-sided test

```
. . tab children_any gender, chi exact
```

children_a			
ny - Do			
you have	gender - What is your		
any	gender?		
children?	Male	Female	Total
0	24	23	47
1	2	6	8
Total	26	29	55

```
      Pearson chi2(1) =    1.8632    Pr = 0.172
      Fisher's exact =                0.257
1-sided Fisher's exact =                0.164
```

Comparison to test of two proportions

```
prtest children_any, by(gender)
```

Two-sample test of proportions

Male: Number of obs = 26

Female: Number of obs = 29

Variable	Mean	Std. Err.	z	P> z	[95% Conf. Interval]
Male	.0769231	.0522589			-.0255026 .1793487
Female	.2068966	.0752216			.0594649 .3543282
diff	-.1299735	.091593			-.3094925 .0495456
under Ho:	.0952197	-1.36	0.172		
diff = prop(Male) - prop(Female) z = -1.3650					
Ho: diff = 0					
Ha: diff < 0 Ha: diff != 0 Ha: diff > 0					
Pr(Z < z) = 0.0861		Pr(Z > z) = 0.1723		Pr(Z > z) = 0.9139	

For 2x2 tables the chi-squared statistic is equal to the z statistic squared

```
. di (-1.365)^2
```

```
1.863
```

Chi-squared test of independence

- The chi-squared test can be used for more than 2 levels of exposure (with a dichotomous outcome)
 - The null hypothesis is $p_1 = p_2 = \dots = p_k$
 - The alternative hypothesis is that not all the proportions are the same
- Note that, like ANOVA, a statistically significant result does not tell you which level differed from the others
- Also when you have more than 2 groups, all tests are 2-sided
- The degrees of freedom for the test are $k-1$

Chi-squared test of independence

```
. tab sex lastalc_3 if hiv==1, row col chi exact
```

```
+-----+
| Key      |
+-----+
| frequency |
| row percentage |
| column percentage |
+-----+
```

Note that this is a 2x3 table,
so the chi-squared test has
1x2=2 degrees of freedom

RECODE of lastalc (E1. Last time took alcohol)				
A1. Sex	Never	>1 year a	Within th	Total
male	110	64	203	377
	29.18	16.98	53.85	100.00
	29.49	35.36	45.72	37.78
female	263	117	241	621
	42.35	18.84	38.81	100.00
	70.51	64.64	54.28	62.22
Total	373	181	444	998
	37.37	18.14	44.49	100.00
	100.00	100.00	100.00	100.00

```
Pearson chi2(2) = 23.2657    Pr = 0.000
Fisher's exact =              0.000
```

Chi-squared test of independence

- Another way to state the null hypothesis for the chi-squared test:
 - Factor A is not associated with Factor B
- The alternative is
 - Factor A is associated with Factor B
- For more than 2 levels of the outcome variable this would make the most sense
- The degrees of freedom are $(r-1)*(c-1)$
(r =rows, c =columns)

Paired dichotomous data

- Matched pairs
 - Matched case-control study
 - Before and after data
- You cannot just put each individual into an exposure and disease box, because then you would lose the benefits of pairing (and the observations would not be independent!)
- Instead you have a table that tabulates each of the 4 possible states for each pair

Paired dichotomous data

- For a 1:1 matched case/control study, in all pairs, one has the disease (case) and the other does not (control). The table then counts the number of pairs in which
 - 1. Both were exposed
 - 2. Neither were exposed
 - 3. The case was exposed, the control was not
 - 4. The case was not exposed, the control was exposed

Example: Case-control study HIV positives on ART in Uganda

- The study question was: Is alcohol consumption in the past 3 months associated with treatment failure?
 - The null hypothesis is that alcohol consumption is not associated with treatment failure
- Cases:
 - Treatment failure: HIV viral load after 6 months of ART >400 copies
- Controls:
 - No treatment failure: HIV viral load <400
- Matched on sex, duration on treatment, and treatment regimen class

```
. list matched_pair lastalc_case lastalc_control
```

	matched~r	lastal~e	lastal~l
1.	1	Yes	No
2.	2	Yes	Yes
3.	3	No	No
4.	4	Yes	No
5.	5	No	No
6.	6	No	Yes
7.	7	Yes	Yes
8.	8	Yes	No
9.	9	No	No
10.	10	No	No
11.	12	Yes	Yes
12.	13	No	Yes
13.	14	Yes	No
14.	15	Yes	No
15.	16	Yes	No
16.	17	No	No
17.	18	No	No
18.	19	No	No
19.	20	Yes	No
20.	21	No	No
21.	22	Yes	No
22.	23	No	No
23.	24	Yes	Yes
24.	25	No	No
25.	26	Yes	No
26.	27	No	Yes
27.	28	No	No

```
. tab lastalc_case lastalc_control
```

lastalc_ca se	lastalc_control		Total
	No	Yes	
No	11	3	14
Yes	9	4	13
Total	20	7	27

Data are in “treatment outcomes case control.dta”

Paired dichotomous data

- The test statistic is

$$X^2 = \frac{[|r - s| - 1]^2}{(r + s)}$$

- r and s are the number of discordant pairs
 - Concordant pairs provide no information
- Under the null hypothesis, r and s would be equal
- This statistic has an approximate Chi-squared distribution with 1 degree of freedom
- The test is called McNemar's test
 - The -1 is a continuity correction, not all versions of the test use this, some use .5

Paired dichotomous data

- $r=9, s=3$
- Test statistic = $(9-3-1)^2/12 = 2.083$

```
. di chi2tail(1,2.083)  
.14894719
```
- Test statistic = $(6)^2/12 = 3$ (Not using the continuity correction)

```
di chi2tail(1,3)  
.08326452
```

In Stata, use mcc for Matched Case Control

```
mcc case_exposed control_exposed  
. . mcc lastalc_case lastalc_control
```

Cases	Controls		Total
	Exposed	Unexposed	
Exposed	4	9	13
Unexposed	3	11	14
Total	7	20	27

McNemar's chi2(1) = 3.00 Prob > chi2 = 0.0833

Exact McNemar significance probability = 0.1460

Proportion with factor

Cases	.4814815			
Controls	.2592593	[95% Conf. Interval]		

difference	.2222222	-.0518969	.4963413	
ratio	1.857143	.9114712	3.78397	
rel. diff.	.3	.0159742	.5840258	
odds ratio	3	.7486845	17.228	(exact)

Use mcci if you only have the table, not the raw data

```
mcci #both_exposed #case_exposed_only #control_exposed_only #neither_exposed  
. mcci 4 9 3 11
```

Cases	Controls		Total
	Exposed	Unexposed	
Exposed	4	9	13
Unexposed	3	11	14
Total	7	20	27

```
McNemar's chi2(1) = 3.00 Prob > chi2 = 0.0833  
Exact McNemar significance probability = 0.1460
```

Proportion with factor

Cases	.4814815			
Controls	.2592593	[95% Conf. Interval]		

difference	.2222222	-.0518969	.4963413	
ratio	1.857143	.9114712	3.78397	
rel. diff.	.3	.0159742	.5840258	
odds ratio	3	.7486845	17.228	(exact)

Paired dichotomous data

- Note that the McNemar test is only for MATCHED data
- It is quite possible to collect unmatched case control data. Then you analyze using the chi-square methods presented earlier.

Paired dichotomous data

- For before and after data, the pairs are the individual participant, and the four outcomes might be:
 1. “Yes” before + “Yes” after (no change)
 2. “No” before + “No” after (no change)
 3. “Yes” before + “No” after
 4. “No” before + “Yes” after
- e.g. Positive biomarker test at baseline and 3 months follow up

Self-reported alcohol consumption in Uganda

McNemar's test for paired data

- Null hypothesis: No change in the proportion PEth+ (≥ 50 ng/ml) from baseline to 3 months in persons entering HIV care in Uganda

```
. tab peth0_50 peth3_50
```

peth0_50	peth3_50		Total
	0	1	
0	78	7	85
1	23	69	92
Total	101	76	177

using BREATH wide data.dta

Paired dichotomous data

Matched case-control study command

```
mcc peth0_50 peth3_50
```

	Controls		
Cases	Exposed	Unexposed	Total
Exposed	69	23	92
Unexposed	7	78	85
Total	76	101	177

McNemar's $\chi^2(1) = 8.53$ Prob > $\chi^2 = 0.0035$
 Exact McNemar significance probability = 0.0052

Proportion with factor

Cases	.519774		
Controls	.4293785	[95% Conf. Interval]	
	-----	-----	-----
difference	.0903955	.0255752	.1552158
ratio	1.210526	1.064678	1.376355
rel. diff.	.1584158	.0609088	.2559229
odds ratio	3.285714	1.36498	9.066655 (exact)

Comparison of disease frequencies across groups

- The chi-squared test and McNemar's test are tests of independence
- They do not give us an estimate of how much the two groups differ, i.e. how much the disease outcome varies by the exposure variable
- We use odds ratios (OR) and relative risks (RR) as measures of ratios of disease outcome (given exposure or lack of exposure)
- The odds ratio and the relative risk are just two examples of “measures of association”

Comparison of disease frequencies – relative risk

	Exposure		
Disease	+	-	Total
+	a	b	a+b
-	c	d	c+d
Total	a+c	b+d	n=a+b+c+d

- Risk ratio (or relative risk or relative rate)
- $$= P(\text{disease} \mid \text{exposed}) / P(\text{disease} \mid \text{unexposed})$$
- $$= R_e / R_u = a/(a+c) / b/(b+d)$$

Comparison of disease frequencies – relative risk

	Exposure		
Disease	+	-	Total
+	a	b	a+b
-	c	d	c+d
Total	a+c	b+d	n=a+b+c+d

- Note that you cannot calculate this entity when you have chosen your sample based on disease status
 - i.e. Case-control study – you have fixed the probability of disease a priori (i.e. usually 50%)! Relative risk is a NO GO!
 - You can calculate it but it won't have any meaning...

Odds and Odds Ratio

- If an event occurs with probability p , the odds of the event are $p/(1-p)$ to 1
- If an event has probability .5, the odds are 1:1
- Conversely, if the odds of an event are $a:b$, the probability of a occurring is $a/(a+b)$
 - The odds of horse A winning over horse B winning are 2:1 $\rightarrow$ the probability of horse A winning is .667.

Odds ratio in a cohort study

	Exposure		
Disease	+	-	Total
+	a	b	a+b
-	c	d	c+d
Total	a+c	b+d	n=a+b+c+d

- Odds of disease among the exposed persons
= $P(\text{disease} \mid \text{exposed}) / (1 - P(\text{disease} \mid \text{exposed}))$
= $[a / (a + c)] / [c / (a + c)] = a/c$
- Odds of disease among the unexposed persons
= $P(\text{disease} \mid \text{unexposed}) / (1 - P(\text{disease} \mid \text{unexposed}))$
= $[b / (b + d)] / [d / (b + d)] = b/d$
- Odds ratio = $a/c / b/d = ad/bc$

Odds ratio

- Note that the odds ratio is also equal to
$$\frac{[P(\text{exposed} \mid \text{disease}) / (1 - P(\text{exposed} \mid \text{disease}))]}{[P(\text{exposed} \mid \text{no disease}) / (1 - P(\text{exposed} \mid \text{no disease}))]}$$
- This is what we calculate for case-control studies because the proportion with disease is fixed (so you can't calculate the probability of disease or the odds of disease)

Interpretation of ORs and RRs

- If the OR or RR equal 1, then there is no effect of exposure on disease.
- If the OR or RR >1 then disease is increased in the presence of exposure. (Risk factor)
- If the OR or RR <1 then disease is decreased in the presence of exposure. (Protective factor)

Comparing measures of association

- When a disease is rare, i.e. the risk is $<10\%$, the odds ratio approximates the risk ratio
- The odds ratio overestimates the risk ratio
- Why use it? – statistical properties, usefulness in case-control studies

The association of having any children with gender

```
tab children_any gender
```

```
children_a |  
  ny - Do |  
  you have | gender - What is your  
    any |      gender?  
children? |      Male      Female |      Total  
-----+-----+-----+-----  
      0 |      24      23 |      47  
      1 |       2       6 |       8  
-----+-----+-----+-----  
Total |      26      29 |      55
```

What is the (estimated) odds ratio (where sex=female is the exposure)?

```
. di (6*24) / (2*23)
```

```
3.1304348
```

95% Confidence interval for an odds ratio

- Remember the 95% confidence interval for a mean μ

Lower Confidence Limit:

$$\bar{X} - 1.96\sigma / \sqrt{n}$$

Upper Confidence Limit:

$$\bar{X} + 1.96\sigma / \sqrt{n}$$

- The odds ratio is not normally distributed (it ranges from 0 to infinity)
 - But the natural log (ln) of the odds ratio is approximately normal
 - The estimate of the standard error of the estimated ln OR is

$$SE(\ln(OR)) = \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}$$

95% Confidence interval for an odds ratio

- We calculate the 95% confidence interval for the log odds

$$\left(\ln OR - 1.96 \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}, \ln OR + 1.96 \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}} \right)$$

- Then exponentiate back to obtain the 95% confidence interval for the OR

$$\left(e^{\left(\ln OR - 1.96 \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}} \right)}, e^{\left(\ln OR + 1.96 \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}} \right)} \right)$$

Calculating an odds ratio and 95% confidence interval in Stata using tabodds command

Tabodds outcomevar exposurevar , or

```
. tabodds children_any gender, or
```

```
-----
```

gender	Odds Ratio	chi2	P>chi2	[95% Conf. Interval]	
Male	1.000000	.	.	.	.
Female	3.130435	1.83	0.1762	0.546769	17.922776

```
-----
```

Test of homogeneity (equal odds): chi2(1) = 1.83
Pr>chi2 = 0.1762

Score test for trend of odds: chi2(1) = 1.83
Pr>chi2 = 0.1762

Calculating an odds ratio and 95% confidence interval in Stata using cc command

```
. gen gender_01=gender-1
```

```
. cc children_any gender_01
```

	Exposed	Unexposed	Total	Proportion Exposed
Cases	6	2	8	0.7500
Controls	23	24	47	0.4894
Total	29	26	55	0.5273
	Point estimate		[95% Conf. Interval]	
Odds ratio	3.130435		.4837995	34.13049 (exact)
Attr. frac. ex.	.6805556		-1.066972	.9707007 (exact)
Attr. frac. pop	.5104167			
chi2(1) = 1.86 Pr>chi2 = 0.1723				

Exact confidence intervals use the hypergeometric distribution

Chi-square test when the exposure has several levels (outcome dichotomous)

- e.g. Is low CD4 count (<250) at HIV testing associated with alcohol consumption category?

•

```
tab cd4_low lastalc_3, col chi
```

cd4_low	RECODE of lastalc (E1. Last time took alcohol)			Total
	Never	>1 year a	Within th	
0	203	89	246	538
	54.42	49.44	55.78	54.12
1	170	91	195	456
	45.58	50.56	44.22	45.88
Total	373	180	441	994
	100.00	100.00	100.00	100.00

Pearson chi2(2) = 2.0894 Pr = 0.352

Odds ratio when the exposure has several levels

- One level is the “unexposed” or reference level

This is as if you partitioned your data off and did a chi-square test comparing cd4<250 in the past drinker versus lifetime abstainer categories

```
. tabodds cd4_low lastalc_3, or
```

lastalc_3	Odds Ratio	chi2	P>chi2	[95% Conf. Interval]	
Never	1.000000	.	.	.	.
>1 year	1.220952	1.21	0.2722	0.854441	1.744676
Within ~r	0.946557	0.15	0.6979	0.717263	1.249151

```
Test of homogeneity (equal odds): chi2(2) = 2.09
Pr>chi2 = 0.3522
```

```
Score test for trend of odds: chi2(1) = 0.19
Pr>chi2 = 0.6623
```

Stata lets you choose the reference level

```
. tabodds cd4_low lastalc_3, or base(2)
```

lastalc_3	Odds Ratio	chi2	P>chi2	[95% Conf. Interval]	
Never	0.819033	1.21	0.2722	0.573172	1.170355
>1 year~o	1.000000	.	.	.	.
Within ~r	0.775261	2.06	0.1509	0.547265	1.098244

Test of homogeneity (equal odds): chi2(2) = 2.09
Pr>chi2 = 0.3522

Score test for trend of odds: chi2(1) = 0.19
Pr>chi2 = 0.6623

Odds ratio for matched pairs

- The odds ratio is r/s
- The standard error of $\ln(OR)$ is

$$SE(\ln[OR]) = \sqrt{\frac{r+s}{rs}}$$

- So the 95% confidence interval for the estimated OR is

$$\left(e^{\left(\ln OR - 1.96 \sqrt{\frac{r+s}{rs}} \right)}, e^{\left(\ln OR + 1.96 \sqrt{\frac{r+s}{rs}} \right)} \right)$$

Odds ratio for matched pairs

- For alcohol vs. case/control status:
- $OR = 9/3 = 3$
- $SE(\ln OR) = \sqrt{(9+3)/27} = .667$
- 95% CI: $\exp(\ln(3) - 1.96 * .667)$,
 $\exp(\ln(3) + 1.96 * .667)$
(0.81 – 11.1)

Data are in: treatment outcomes case control.dta

In Stata

```
mcc case_exposed control_exposed
. . mcc lastalc_case lastalc_control
```

	Controls		
Cases	Exposed	Unexposed	Total
Exposed	4	9	13
Unexposed	3	11	14
Total	7	20	27

```
McNemar's chi2(1) =      3.00      Prob > chi2 = 0.0833
Exact McNemar significance probability      = 0.1460
```

Proportion with factor

```
Cases      .4814815
Controls    .2592593      [95% Conf. Interval]
-----
difference  .2222222      -.0518969      .4963413
ratio       1.857143      .9114712      3.78397
rel. diff.   .3          .0159742      .5840258
```

```
odds ratio      3      .7486845      17.228      (exact)
```