

Metabolic Dynamics – Kinetics and Transport Measured by 1 and 2D NMR Spectroscopy, Modeling metabolic flux

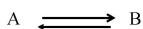
Chemical Exchange in NMR

- Chemical exchange in NMR refers to any process in which a nucleus exchanges between two or more environments in which its NMR parameters (chemical shift, scalar coupling, dipolar coupling, relaxation rate) differ.
- Chemical exchange in NMR can be a curse or rewarding – its influence can cause signals to become invisible beyond detection or it can allow one to uncover a large range of motional properties at every site within a molecule ...

Types of Chemical Exchange

Intramolecular exchange

- Motions of sidechains in proteins
- Helix-coil transitions of nucleic acids
- Unfolding of proteins

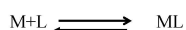


Conformational equilibria



Intermolecular exchange

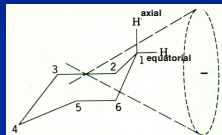
- Binding of small molecules to macromolecules
- Protonation/deprotonation equilibria
- Isotope exchange processes
- Enzyme catalyzed reactions



Because NMR detects the molecular motion itself, rather than the numbers of molecules in different states, NMR is able to detect chemical exchange even when the system is in equilibrium

Conformational Equilibrium

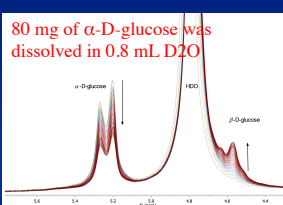
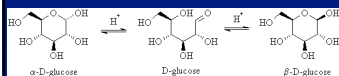
- ❖ Chemical shift equivalence is also caused by rapid exchange mechanisms (faster than once in 10^{-3} sec.).
 - For example, the chemical shift of the cyclohexane protons is an average of the shifts of the axial and equatorial protons. At room temperature, the spectrum consists of a singlet at 1.42 ppm, the average of the axial and equatorial chemical shifts.



The equatorial protons would be more deshielded than the axial protons if there was not a rapid exchange of these two positions.

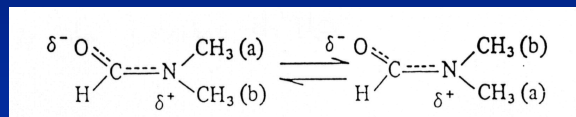
Conformational Equilibrium

- ❖ Non-equivalence – E.g. Mutarotation of carbohydrates
- ❖ The α - and β - anomers of carbohydrates are typically stable solids. However, in aqueous solution, they quickly equilibrate to a mixture of the two forms.
 - ❖ For example, in aqueous solution, glucose exists as a mixture of 36% α - and 64% β - (>99% of the pyranose forms exist in solution).



Conformational Equilibrium

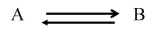
- At room temperature, N,N-dimethylformamide shows 2 CH_3 peaks, because of the rate of rotation around the hindered C–N bond is slow on the NMR time scale.
- However, as one raises the temperature the barrier to rotation is overcome and the two CH_3 peaks merge into a single peak at $\approx 123^\circ\text{C}$.



Types of Chemical Exchange

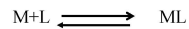
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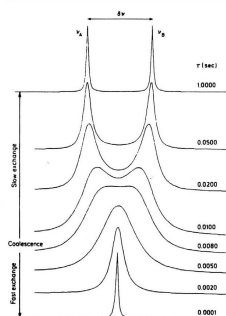
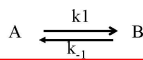
NMR Time Scale

Time Scale Chem. Shift, δ Coupling Const., J T2 relaxation

Slow	$k \ll \delta_A - \delta_B$	$k \ll J_A - J_B$	$k \ll 1/T_{2A} - 1/T_{2B}$
Intermediate	$k = \delta_A - \delta_B$	$k = J_A - J_B$	$k = 1/T_{2A} - 1/T_{2B}$
Fast	$k \gg \delta_A - \delta_B$	$k \gg J_A - J_B$	$k \gg 1/T_{2A} - 1/T_{2B}$
Sec ⁻¹	0 - 1000	0 - 12	1 - 20

- NMR time-scale refers to the chemical shift timescale.
- The range of the rate can be studied 0.05-5000 s⁻¹ for H can be extended to faster rate using ¹⁹F, ¹³C and etc.

2-state First Order Exchange



Lifetime of state A:

$$\tau_A = 1/k_{+1}$$

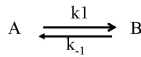
Lifetime of state B:

$$\tau_B = 1/k_{-1}$$

Use a single lifetime

$$\begin{aligned} 1/\tau &= 1/\tau_A + 1/\tau_B \\ &= k_{+1} + k_{-1} \end{aligned}$$

Slow Exchange $k \ll \delta_A - \delta_B$



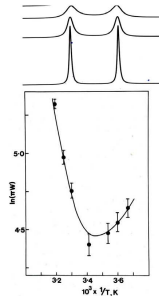
- Separate lines are observed for each state.
- The exchange rate can be readily measured from the line widths of the resonances
- Like the apparent spin-spin relaxation rates, $1/T_{2i,obs}$

$$1/T_{2A,obs} = 1/T_{2A} + 1/\tau_A = 1/T_{2A} + 1/k_1$$

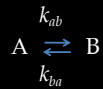
$$1/T_{2B,obs} = 1/T_{2B} + 1/\tau_B = 1/T_{2B} + 1/k_{-1}$$

$$\text{line width } Lw = 1/\pi T_2 = 1/\pi T_2 + k_1/\pi$$

Each resonance is broadened by $\Delta Lw = k/\pi$
Increasing temperature k increases, line width increases



Chemical Exchange Dynamics: 2 site, 1st order case



$$M_a \sim [A]$$

Magnetization proportional to concentration

$$M_a = M_{a,0} e^{i\omega_a t} e^{-t/T_2}$$

Off Resonance and Relaxation

$$\dot{M}_a = \left(-k_{ab} + i\omega_a - \frac{1}{T_{2,a}} \right) M_a + k_{ba} M_b$$

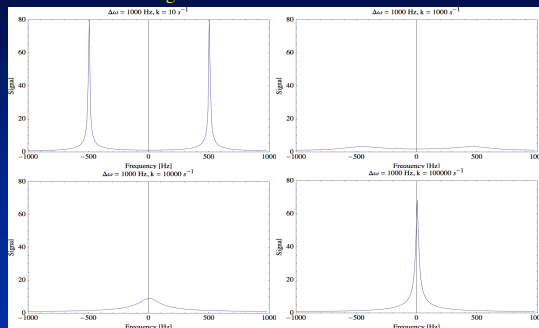
Combined with exchange gives Bloch McConnell Equations

$$\dot{M}_b = \left(-k_{ba} + i\omega_b - \frac{1}{T_{2,b}} \right) M_b + k_{ab} M_a$$

$$\begin{pmatrix} \dot{M}_a \\ \dot{M}_b \end{pmatrix} = \begin{pmatrix} -k_{ab} + i\omega_a - \frac{1}{T_{2,a}} & k_{ba} \\ k_{ab} & -k_{ba} + i\omega_b - \frac{1}{T_{2,b}} \end{pmatrix} \begin{pmatrix} M_a \\ M_b \end{pmatrix}$$

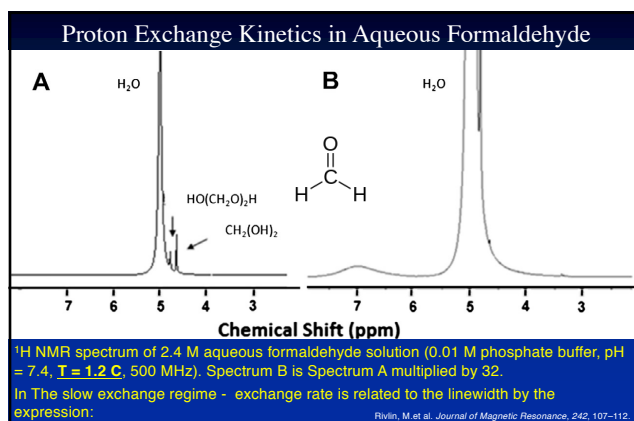
Bloch McConnell Exchange Calculations

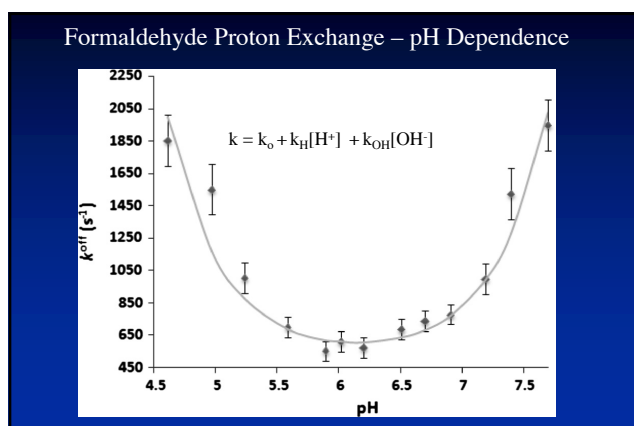
Slow Exchange

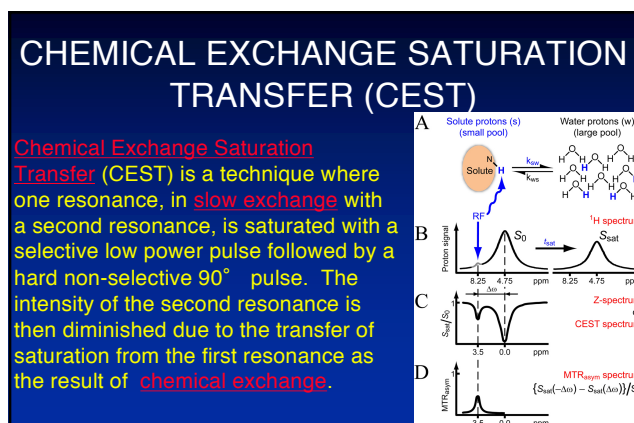


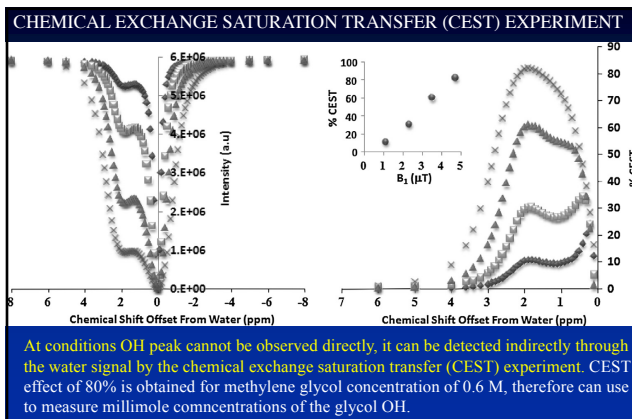
Intermediate Exchange

Fast Exchange









Another Exchange Effect: Selective 180° Pulse

$$\begin{array}{ccc}
 A & \xrightleftharpoons[k_{XA}]{k_{AX}} & X \\
 \downarrow 1/T_{1A} \text{ relaxation} & & \downarrow 1/T_{1X} \text{ relaxation}
 \end{array}$$

Z-MAGNETIZATION

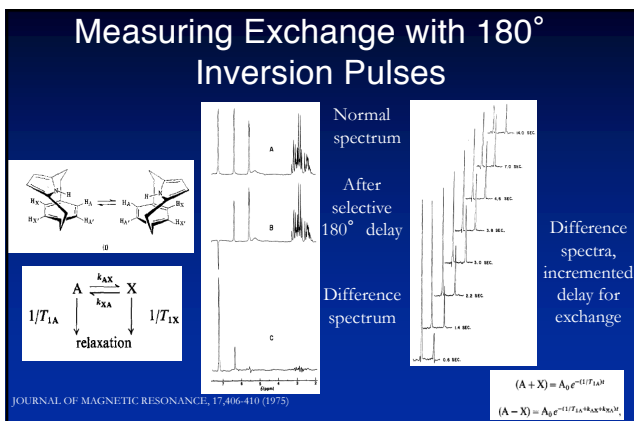
① 1ST 180° PULSE

② CHEMICAL EXCHANGE

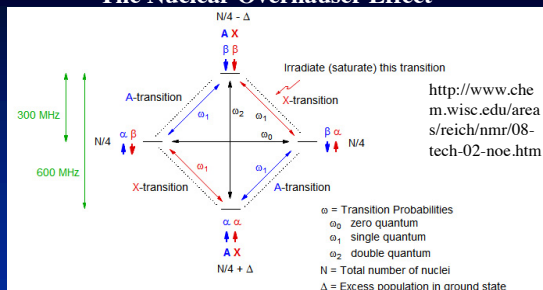
2nd resonance decreases due to exchange

If z-magnetization of each species is inverted relative to the other, exchange will lead to a decrease in total z-magnetization

- Inverted spins of one species exchange between pools, depleting z-magnetization of other species
- Subsequent measurement of other species will give lower signal than expected



The Nuclear Overhauser Effect



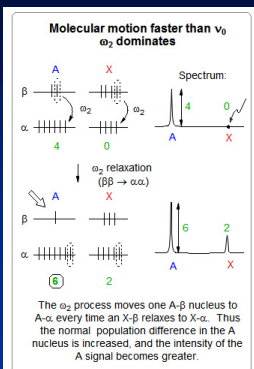
When the X-transition is irradiated, the populations of the $\alpha\alpha$ and $\beta\beta$ states become equalized (saturated), as do the $\beta\alpha$ and $\alpha\beta$ states. As relaxation occurs, the difference in these two populations depends crucially on which of the three relaxation processes dominates.

If $\omega_2 \gg \omega_1, \omega_0$ then the $\beta\alpha/\beta\beta$ population will tend to that of the $\beta\beta$ state, and the $\alpha\beta/\alpha\alpha$ states will tend that of the $\alpha\alpha$ state, hence there will be a larger population difference for the A transition (2Δ) than the equilibrium difference (Δ).

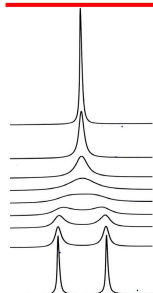
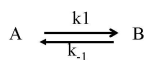
The Nuclear Overhauser Effect

The alteration of normal spin population of a nucleus **X** by irradiation will cause the populations (and hence signal intensities) of other (non-irradiated) nuclei (**A**) to change provided that **X** is causing T_1 relaxation of **A** by the dipole-dipole mechanism.

For the ω_2 process, each time an X nucleus relaxes from β to α state, and A nucleus also undergoes a β to α transition ($\beta\beta \rightarrow \alpha\alpha$). This has the effect of increasing the population difference of A, i.e. an increase the area of A. This is a positive NOE.



Fast Exchange $k \gg \delta_A - \delta_B$



A single resonance is observed, whose chemical shift is the weight average of the chemical shifts of the two individual states

$$\delta_{\text{obs}} = f_A \delta_A + f_B \delta_B, \quad f_A + f_B = 1$$

For very fast limit

$$1/T_{2,\text{obs}} = f_A/T_{2A} + f_B/T_{2B}$$

For moderately fast

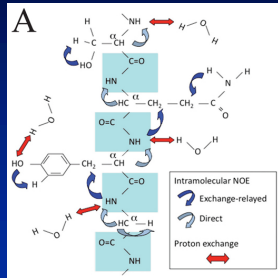
$$1/T_{2,\text{obs}} = f_A/T_{2A} + f_B/T_{2B} + f_A f_B^2 4\pi (\Delta\delta_{AB})^2 / k_{-1}$$

Maximal line broadening is observed when

$$f_A = f_B = 0.5$$

Application to protein dynamics/binding

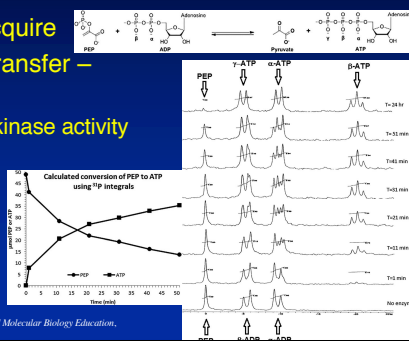
Possible pathways in a mobile protein that can be probed with NMR. Chemical exchange (red) and cross relaxation (blue) occur, the latter either exchange-relayed or through direct excitation of C(α) protons.



van Zijl et al., Magn. Reson. Med. 2003;49:440-449.

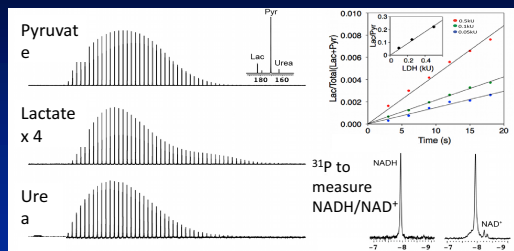
Enzyme kinetics

- Simple pulse-acquire
- Magnetization transfer – saturation
 - ^{31}P – Creatine kinase activity *in vivo*



Werner, R. M., & Johnson, A. (2017). *Biochemistry and Molecular Biology Education*, 45(6), 509-514.

Enzyme Kinetics

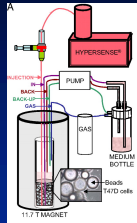
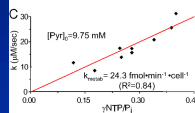
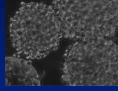


10mm Bioreactor: LDH microspheres: 0.5 kU/mL, 0.1 kU/mL, 0.05 kU/mL
1mL HP [^{13}C] pyruvate (7 mM), urea (20mM) injected over 30s. TR=3s FA=10°, 37° C

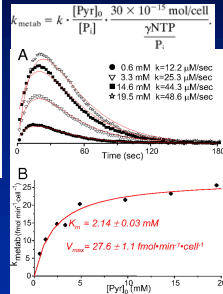
- Linear characteristics of initial rates of reaction – LDH encapsulated consistently

Micro-carrier beads MR bioreactors – reaction

Scheme of the traditional perfusion system with cells grown on Biosilon polystyrene beads

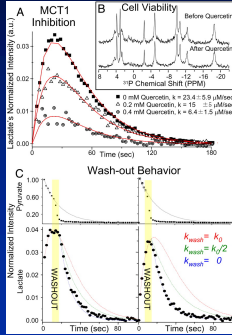


Talia Harris et al. PNAS 2009;106:18131-18136



Microcarrier beads MR bioreactors – rate limiting factor

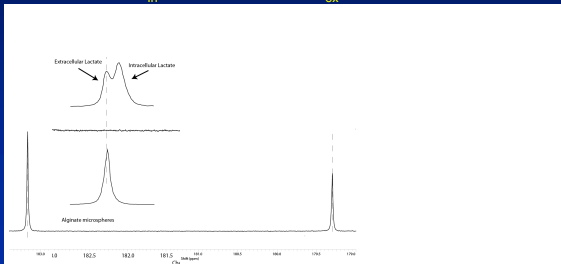
Talia Harris et al. PNAS 2009;106:18131-18136



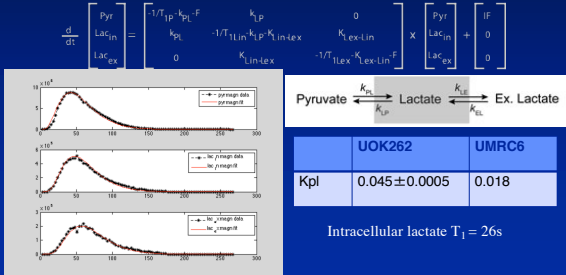
- MCT1 inhibition - Repeated aliquots of 5.9 mM hyperpolarized $^{13}\text{C}_1$ -pyruvate into batches of T47D cells, to whose perfusing media the indicated concentrations of inhibitor were coadded
- ^{31}P NMR spectra showing the constant viability
- Washout experiments – Simulations of pyruvate-to-lactate conversion whose rate remains unaffected by the washing out ($k_{\text{wash}} = k_0$, gray Upper and red Lower); a conversion whose rate is halved vis-à-vis its original level ($k_{\text{wash}} = k_0/2$, green Lower); or a conversion whose rate goes suddenly to zero upon restarting the perfusion ($k_{\text{wash}} = 0$, blue Lower).

Simultaneous observation of the lactate pools in UOK262 cells

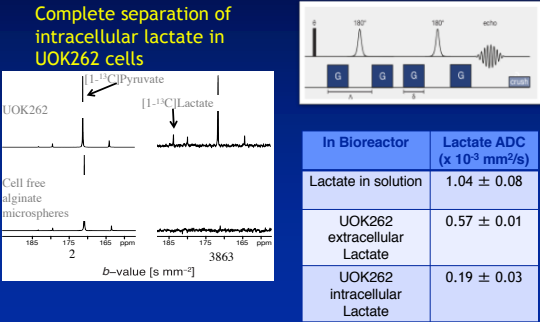
- Lac_{in} : 183.13 ± 0.006 and Lac_{ex} : 183.15 ± 0.006
- LWHM - Lac_{in} : 4.3 ± 0.1 and Lac_{ex} : 2.5 ± 0.07 Hz



Kinetic modeling of bioreactor data

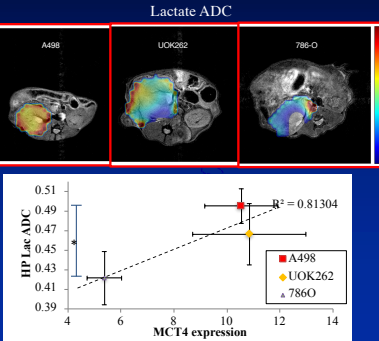


Diffusion weighted HP ¹³C MR in bioreactor



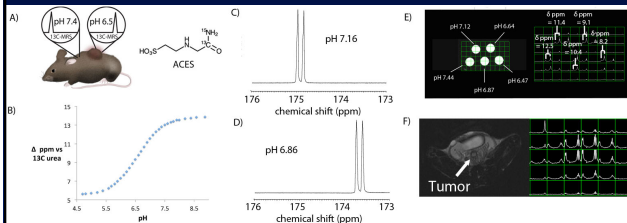
Diffusion weighted hyperpolarized MR *in vivo* to study transport in real time

Lactate ADC calculated using 4 b values (R²>0.7)
High MCT4 -> higher efflux
-> higher lactate ADC





Hyperpolarized ^{13}C ACES pH Imaging



- ACES has a pH dependent chemical shift change over the physiologic range (A-D).
- Co-polarize and use ^{13}C Urea as a chemical shift reference

Hyperpolarized ^{13}C Bicarbonate pH Imaging

