

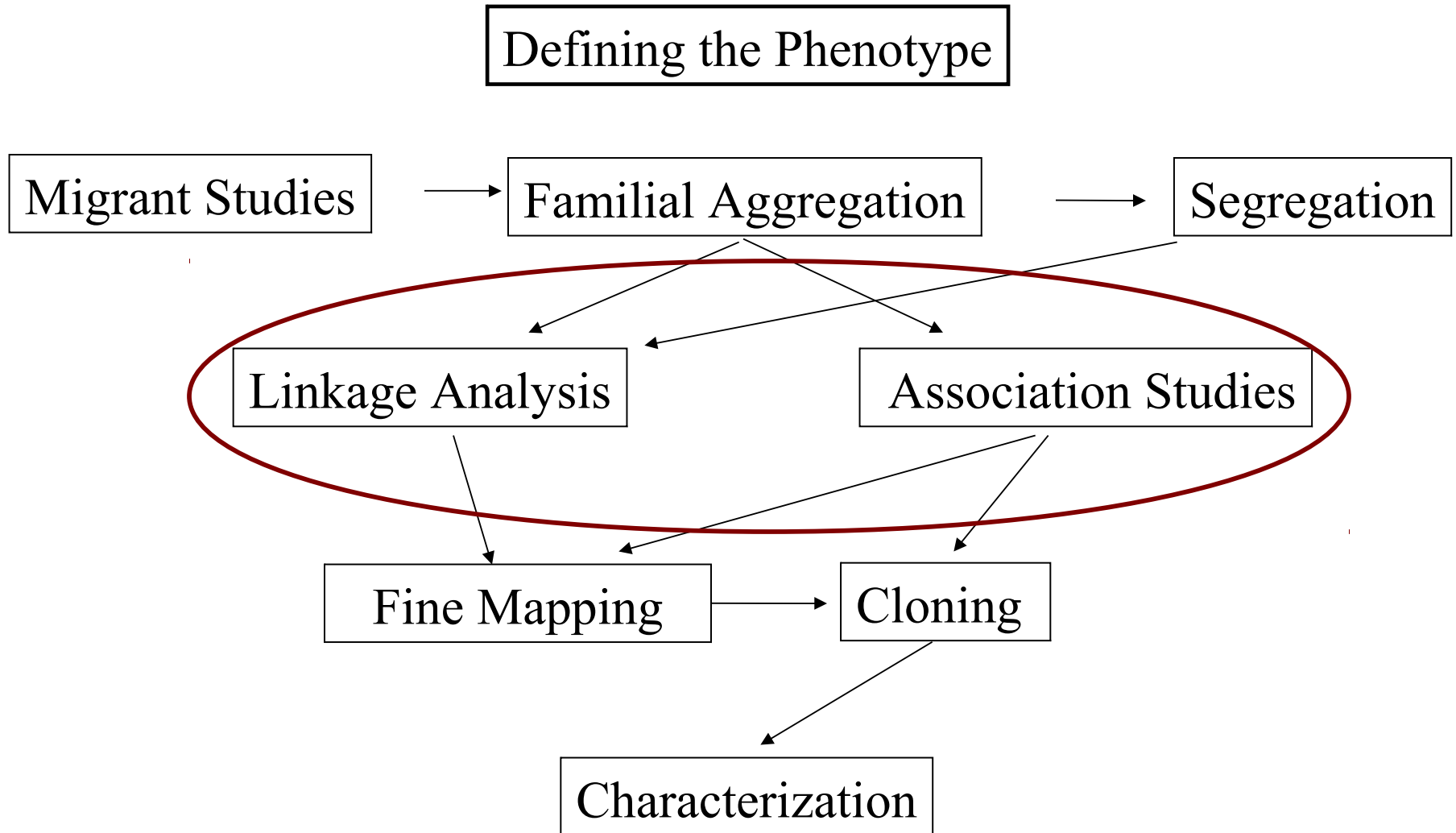
# Family-Based Studies

*“If you cannot get rid of the family skeleton, you may as well make it dance” (G.B. Shaw)*

# Outline

- Review last weeks homeworks
- **Last few topics from previous pop gen lecture**
  - (Had just finished HWE game)
  - **Population stratification**
- Linkage analysis, with PTC testing example
- Family-based association tests
  - Overview
  - Trios/TDT
  - Discordant sibships

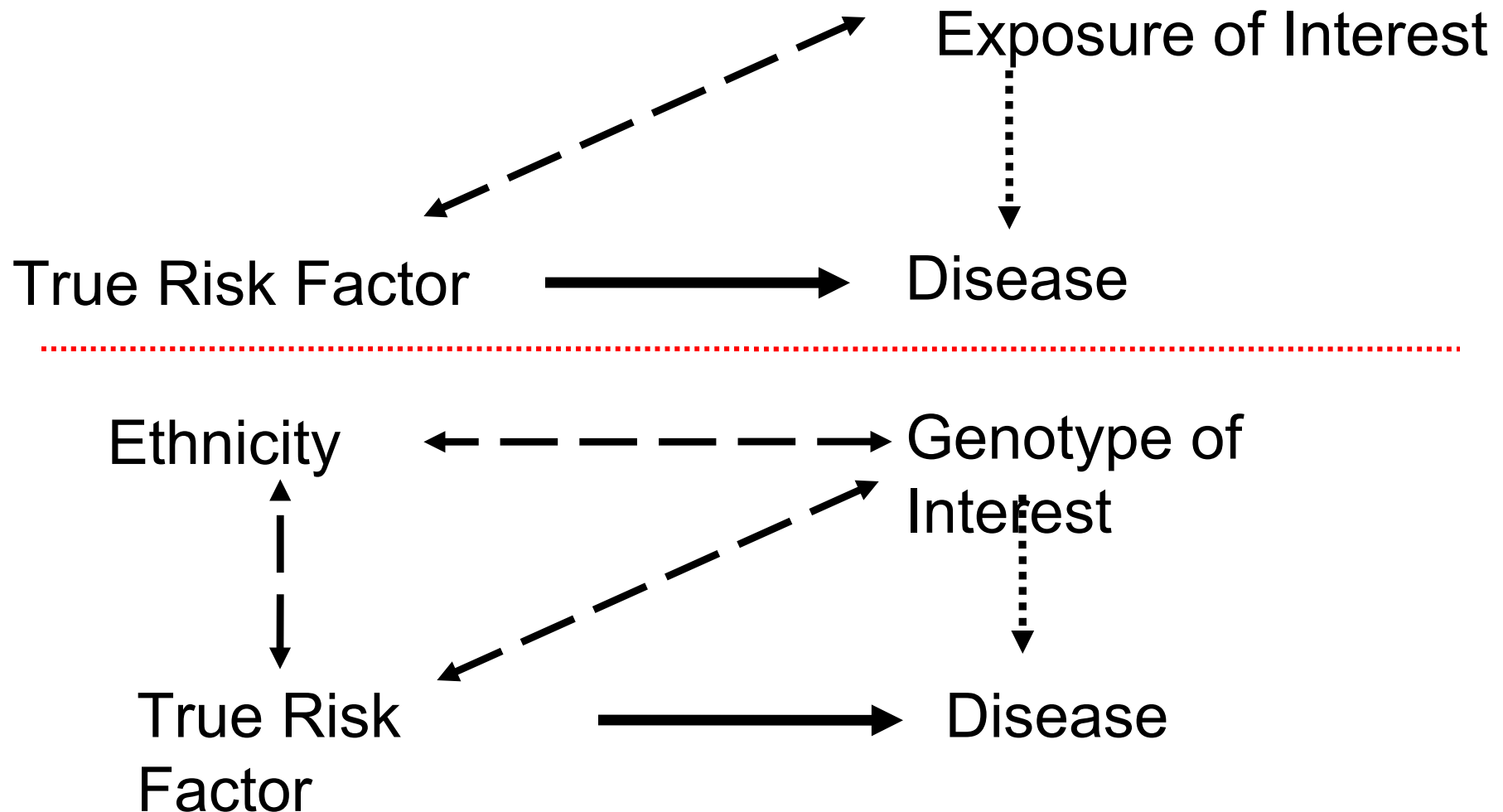
# Process of Genetic Epidemiology



# Population stratification

**Population stratification** is a form of confounding in genetic studies where a gene under study shows marked variation in allele frequency across subgroups of a population and these subgroups differ in their baseline risk of disease

# Population Stratification: Confounding



**Population Stratification: Gm3;5,13,14 in admixed sample of Native Americans of the Pima and Papago tribes**

Study Population: 4,290 Pima and Papago Indians

Genetic Variant: Gm 3;5,13, 15 haplotype (Gm system of human immunoglobulin G)

Outcome: Type 2 diabetes

Question: Is the Gm 3; 5,13, 15 haplotype associated with Type 2 diabetes?

# Population Stratification: Gm3;5,13,14 in admixed sample of Native Americans of the Pima and Papago tribes & Non-insulin dependent Diabetes Mellitus (NIDDM)

Full heritage American Indian population:

|                   | +   | -    |
|-------------------|-----|------|
| Gm3;4,13,14       | ~1% | ~99% |
| NIDDM prevalence: | 40% |      |

Caucasian population:

|                   | +    | -    |
|-------------------|------|------|
| Gm3;4,13,14       | ~66% | ~34% |
| NIDDM prevalence: | 15%  |      |

Combined:

| Gm3,5,13,14 | Case  | Control |
|-------------|-------|---------|
| +           | 7.8%  | 29.0%   |
| -           | 92.2% | 71.0%   |

Different genotype frequency, different phenotype frequency  
Unadjusted for ethnic background OR=0.27 (95% CI 0.18-0.40)

# Population Stratification: Gm3;5,13,14 in admixed sample of Native Americans of the Pima and Papago tribes & Non-insulin dependent Diabetes Mellitus (NIDDM)

| Index of Indian Heritage | Gm3;5,13,14 haplotype | % Diabetes |
|--------------------------|-----------------------|------------|
| 0                        | 65.8%                 | 18.5%      |
| 4                        | 21.1%                 | 28.5%      |
| 8                        | 1.6%                  | 39.2%      |

Combined:

| Gm3,5,13,14 | Case  | Control |
|-------------|-------|---------|
| +           | 7.8%  | 29.0%   |
| -           | 92.2% | 71.0%   |

Different genotype frequency, different phenotype frequency  
Unadjusted for ethnic background, OR=0.27 (95% CI 0.18-0.40)  
Adjusted for ethnic background, OR=0.83 (95%CI 0.58-1.18)

--> Previous result just picked out race/ethnicity!

# Ancestry Informative Markers

- Polymorphisms with known allele frequency differences across ancestral groups
- Useful in estimating ancestry in admixed individuals
- Example: Duffy locus (codes for blood group)
  - 100% sub-Saharan Africans vs. other groups
  - protects *P. vivax* (malaria)

# Example AIM: Duffy locus (rs2814778)

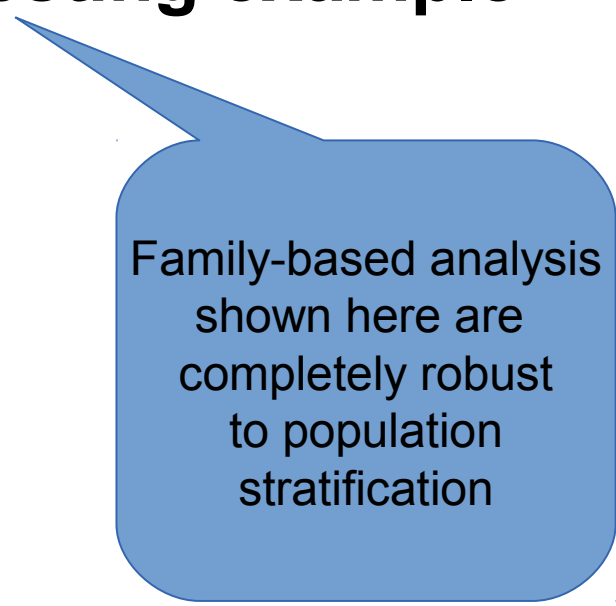
| ss#                                             | Sample Ascertainment                                                                   |                  |                    |        | Genotype Detail |       |   |       |       | Alleles |       |
|-------------------------------------------------|----------------------------------------------------------------------------------------|------------------|--------------------|--------|-----------------|-------|---|-------|-------|---------|-------|
|                                                 | Population                                                                             | Individual Group | Chrom. Sample Cnt. | Source | A/A             | A/G   | G | G/G   | HWP   | A       | G     |
| <a href="#">ss105436776</a> <a href="#">P1</a>  | 24 African/African American, 31 Caucasian, 23 Hispanic, 24 Pacific Rim                 |                  | 204                | GF     | 0.706           | 0.118 |   | 0.176 | 0.001 | 0.765   | 0.235 |
|                                                 | <a href="#">CAUC1</a>                                                                  |                  | 62                 | GF     | 1.000           |       |   |       |       | 1.000   |       |
|                                                 | <a href="#">AFR1</a>                                                                   |                  | 48                 | GF     |                 | 0.292 |   | 0.708 | 0.752 | 0.146   | 0.854 |
|                                                 | <a href="#">HISP1</a>                                                                  |                  | 46                 | GF     | 0.783           | 0.174 |   | 0.043 | 0.273 | 0.870   | 0.130 |
|                                                 | <a href="#">PAC1</a>                                                                   |                  | 48                 | GF     | 0.958           | 0.042 |   |       | 1.000 | 0.979   | 0.021 |
|                                                 | <a href="#">HAPMAP-ASW</a>                                                             |                  | 98                 | IG     | 0.041           | 0.327 |   | 0.633 | 1.000 | 0.204   | 0.796 |
|                                                 | <a href="#">HAPMAP-LWK</a>                                                             |                  | 180                | IG     |                 | 0.011 |   | 0.989 | 1.000 | 0.006   | 0.994 |
|                                                 | <a href="#">HAPMAP-MEX</a>                                                             |                  | 100                | IG     | 0.920           | 0.080 |   |       | 1.000 | 0.960   | 0.040 |
|                                                 | <a href="#">HAPMAP-MKK</a>                                                             |                  | 286                | IG     | 0.007           | 0.126 |   | 0.867 | 0.752 | 0.070   | 0.930 |
|                                                 | <a href="#">HAPMAP-TSI</a>                                                             |                  | 176                | IG     | 0.977           | 0.023 |   |       | 1.000 | 0.989   | 0.011 |
| <a href="#">P3</a>                              | 76 African/African American, 66 Caucasian, 49 Native American/Hispanic, 58 Pacific Rim |                  | 582                | GF     | 0.737           | 0.019 |   | 0.244 | 0.001 | 0.746   | 0.254 |
|                                                 | <a href="#">CAUC3</a>                                                                  |                  | 122                | GF     | 0.984           | 0.016 |   |       | 1.000 | 0.992   | 0.008 |
|                                                 | <a href="#">AFR3</a>                                                                   |                  | 148                | GF     | 0.095           | 0.027 |   | 0.878 | 0.001 | 0.108   | 0.892 |
|                                                 | <a href="#">HISP3</a>                                                                  |                  | 92                 | GF     | 0.957           | 0.043 |   |       | 1.000 | 0.978   | 0.022 |
|                                                 | <a href="#">PAC3</a>                                                                   |                  | 170                | GF     | 1.000           |       |   |       |       | 1.000   |       |
|                                                 | <a href="#">ENSEMBL_Watson</a>                                                         |                  | 2                  | IG     | 1.000           |       |   |       |       | 1.000   |       |
|                                                 | <a href="#">ENSEMBL_Venter</a>                                                         |                  | 2                  | IG     | 1.000           |       |   |       |       | 1.000   |       |
| <a href="#">ss119047871</a> <a href="#">YRI</a> |                                                                                        |                  | 2                  | IG     |                 |       |   | 1.000 |       | 1.000   |       |
| <a href="#">ss164197181</a> <a href="#">YRI</a> | Sub-Saharan African 2                                                                  |                  |                    | IG     |                 |       |   | 1.000 |       | 1.000   |       |

Malaria resistance

<http://www.ncbi.nlm.nih.gov/projects/SNP>

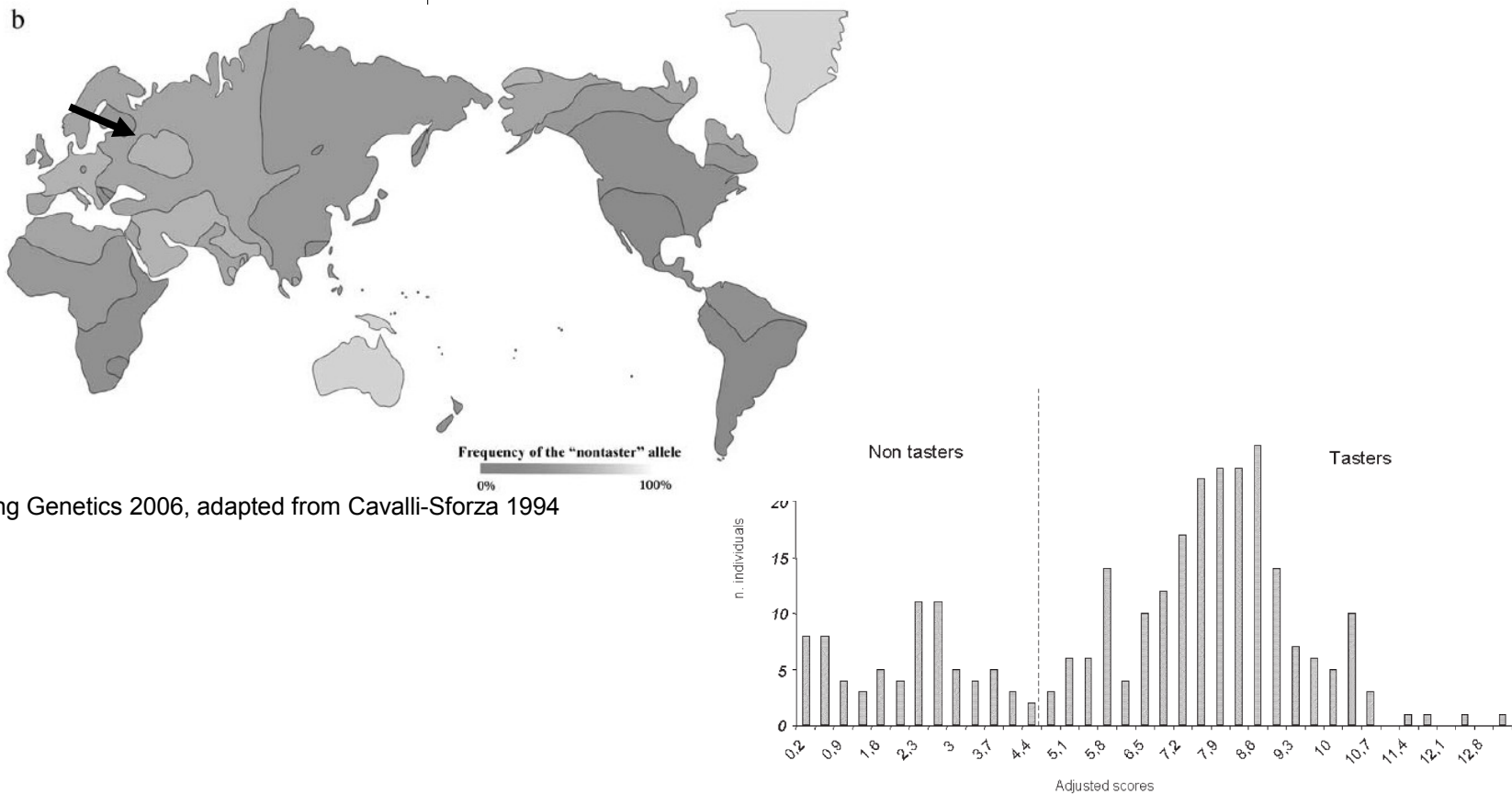
# Outline

- Review last weeks homeworks
- Last few topics from previous pop gen lecture
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- **Linkage analysis, with PTC testing example**
- Family-based association tests
  - Overview
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Family-based analysis shown here are completely robust to population stratification

# Geographic Distribution of PTC Phenotype



Wooding Genetics 2006, adapted from Cavalli-Sforza 1994

**Figure 1** Distribution of PTC sensitivity in Talana. The x-axis indicates the PTC scores, adjusted for age and sex using the following formula:  $n + [(a - a_M) / 20] - 0.73$  female, where  $n$  is the PTC tasted solution,  $a$  is the age of the individual and  $a_M$  is the average age of participants. The value of 0.73 was deducted in females since women are 0.73 dilution steps more sensitive than men at all ages. Distribution of corrected PTC scores showed significant bimodality with a cut-off value of 4.5 that separates the group of tasters from the group of non-tasters, with estimated means of 2.19 (SD = 1.12) and 7.99 (SD = 1.44), respectively.

# First PTC Family Study

|                                        | Number of Familie | Children  |               |
|----------------------------------------|-------------------|-----------|---------------|
|                                        |                   | Can taste | Can not taste |
| Both parents can taste                 | 40                | 90        | 16            |
| One parent can taste, the other can no | 51                | 80        | 37            |
| Neither parent can taste               | 9                 | 0         | 17            |

L. H. Snyder Science 1931

# Types of Genetic Studies

## Family Studies

Compare trait values across family members

## Linkage Analysis

Compare trait values with inheritance patterns

## Association

Compare trait values against genetic variants

# Family Studies

## Familial Relationships

Twins

Siblings

Parents/offspring

## Phenotype information

Affected/Unaffected (Prostate Cancer)

Quantitative measure (Blood Pressure)

No Genotype information required

# Why do Family Studies?

Is the trait genetic?

What is the mode of transmission?

Dominant

Recessive

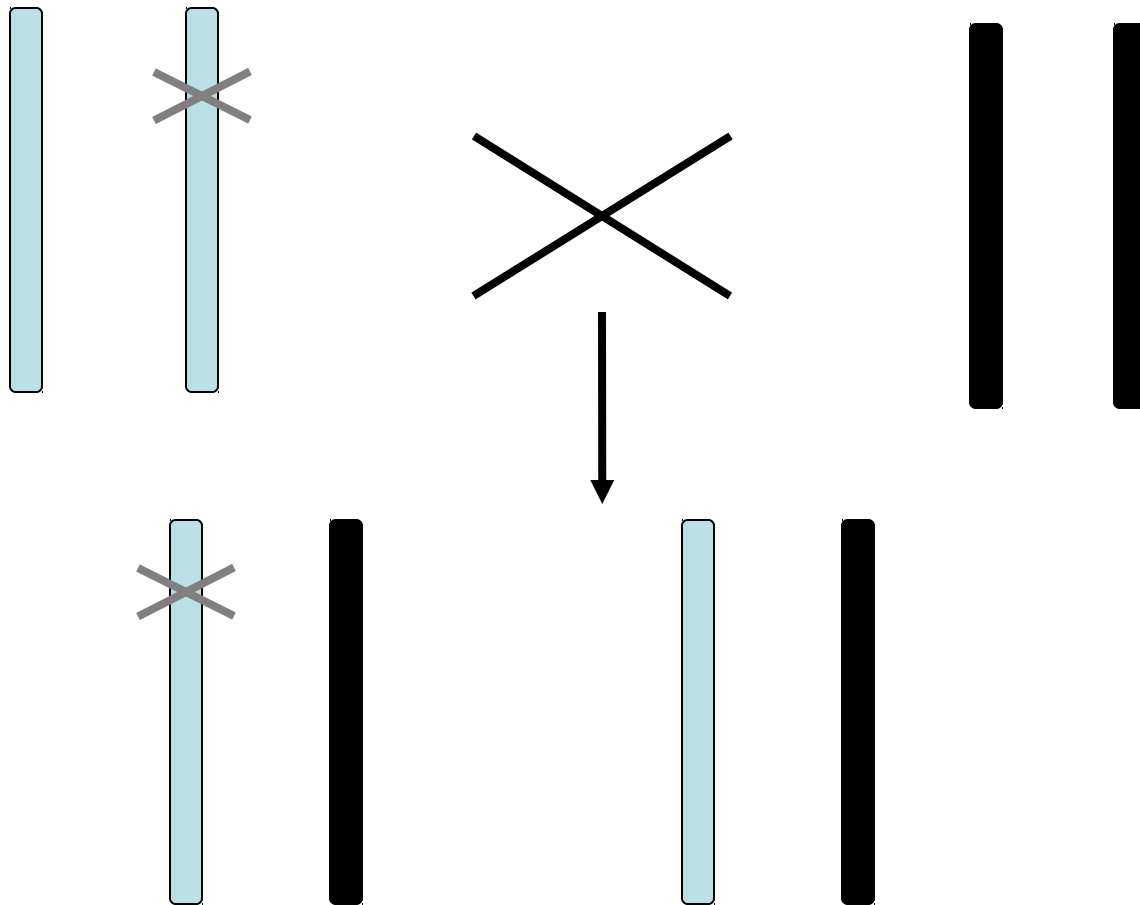
Additive

Polygenic (Multiple genes involved)

# Mendel's laws

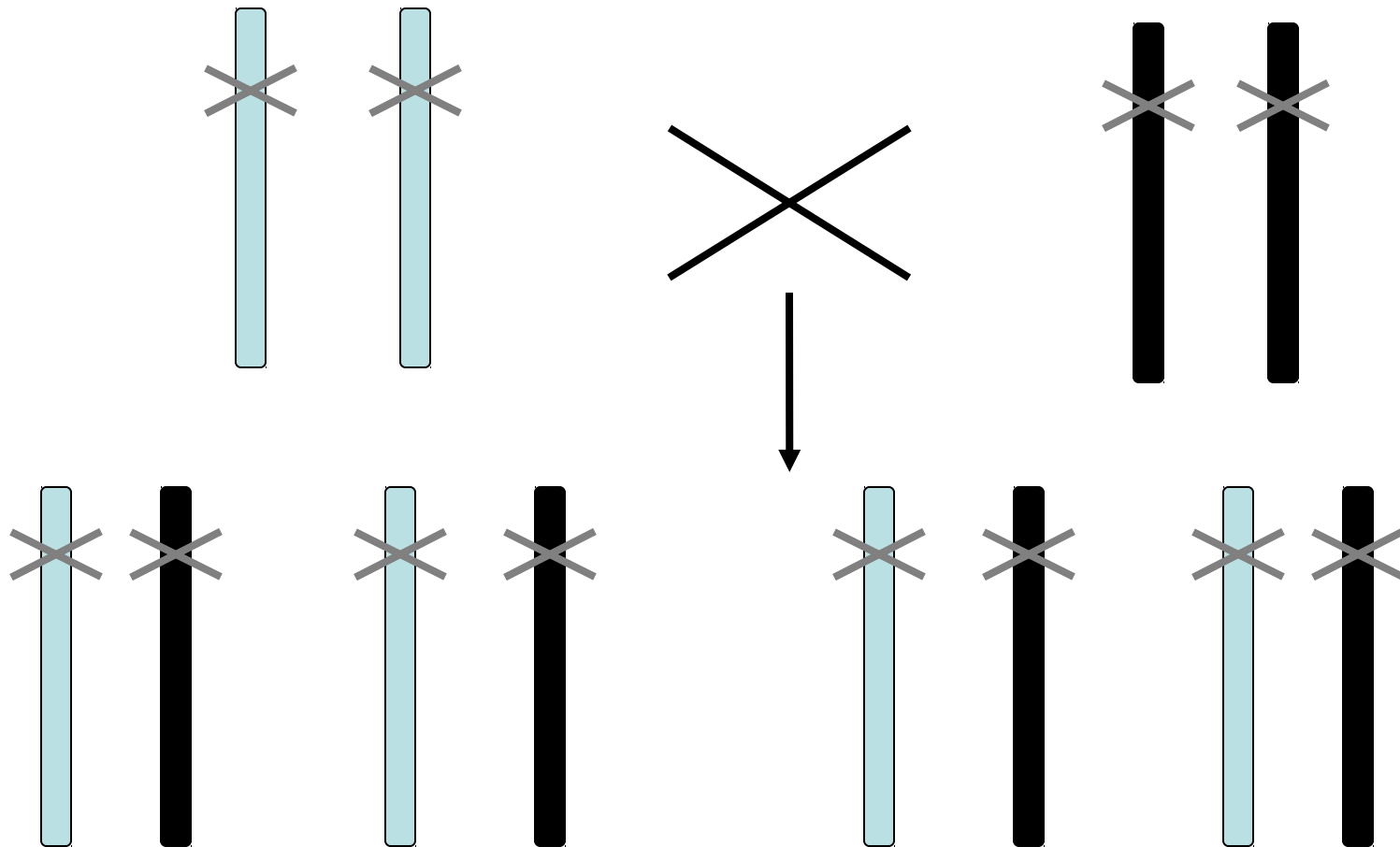
- Recall the playing cards example...
- One allele from each parent for each gene
  - Many family based tests based on this, rather than estimating allele frequencies (case-control)

# Recall: Mutation and Meiosis



# Recall: E.g., Recessive trait

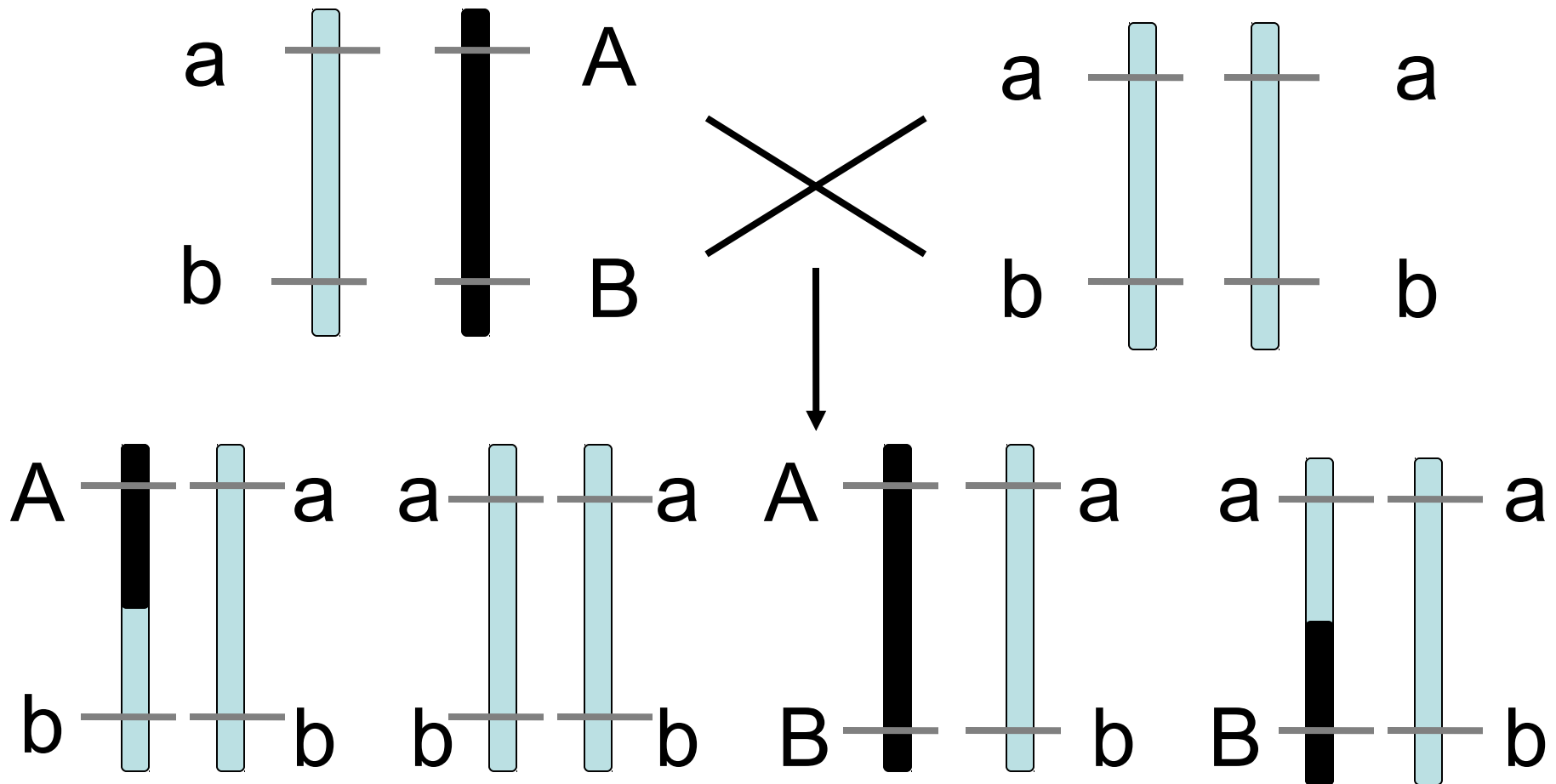
(Know the trait, know the genotype at the disease loci)



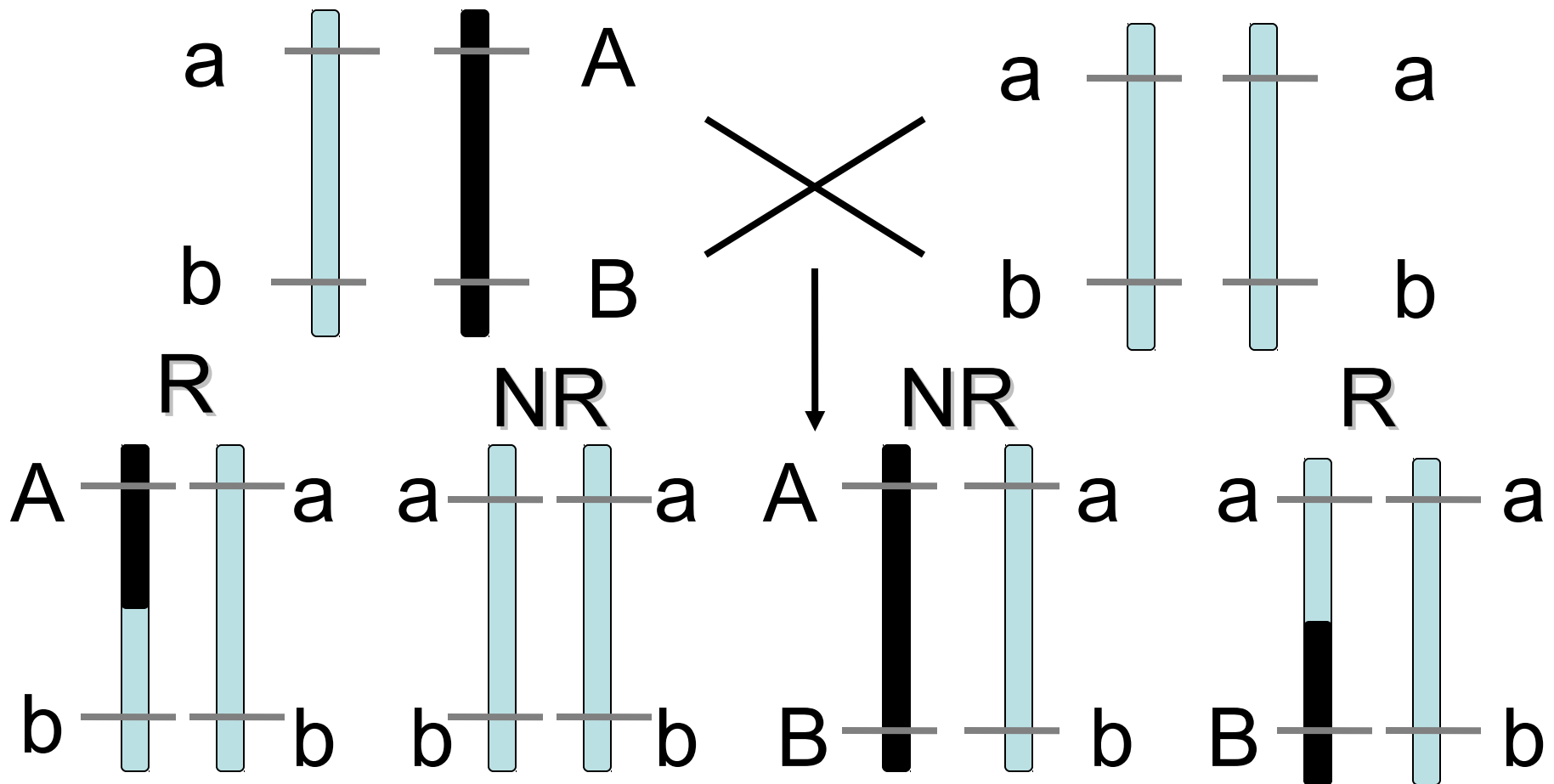
# Linkage Analysis

- Narrow down position of disease gene
- No biological knowledge needed
- Genetic markers (not disease gene)
- Recombination

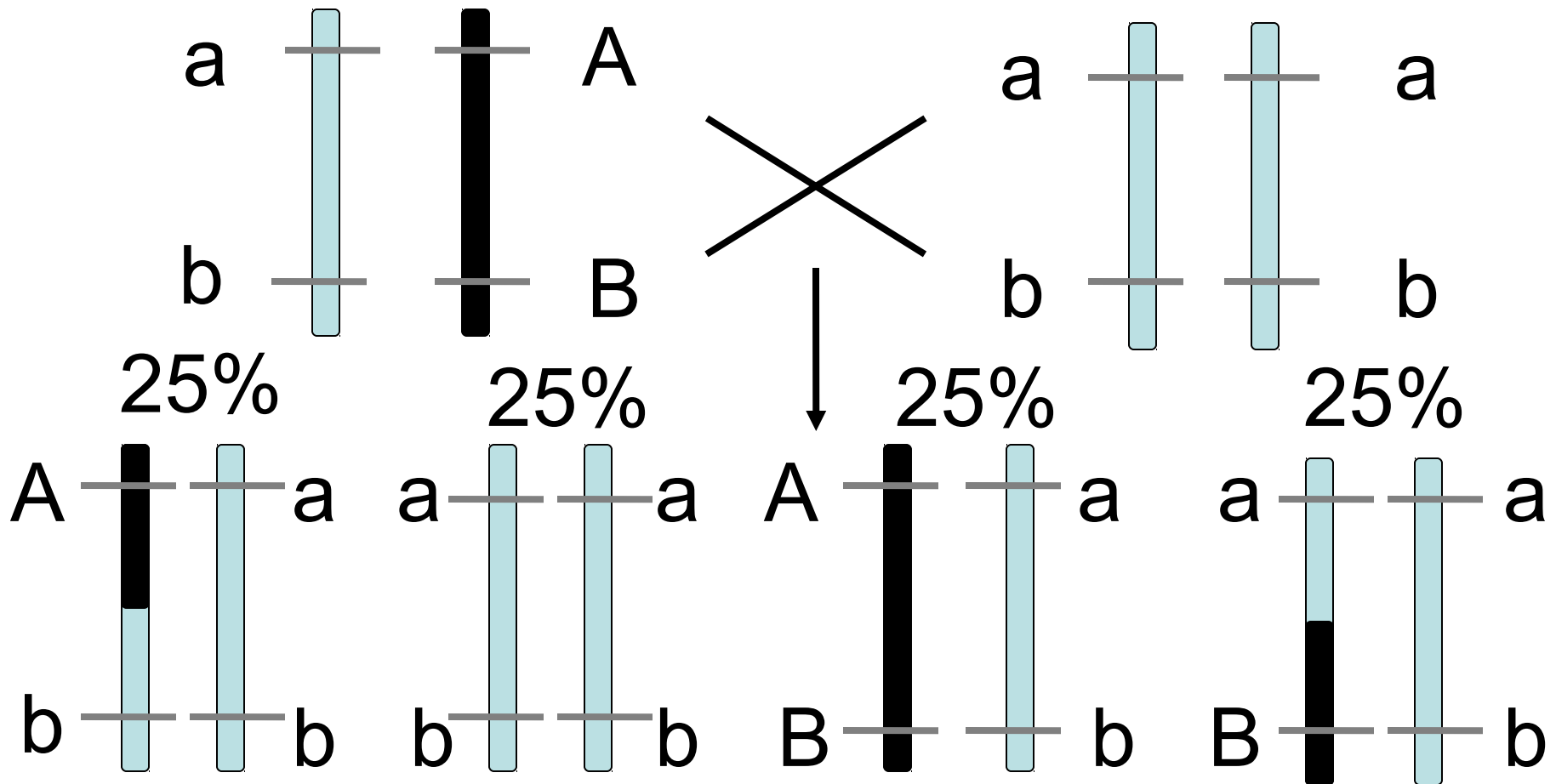
# Recombination – was there recombination?



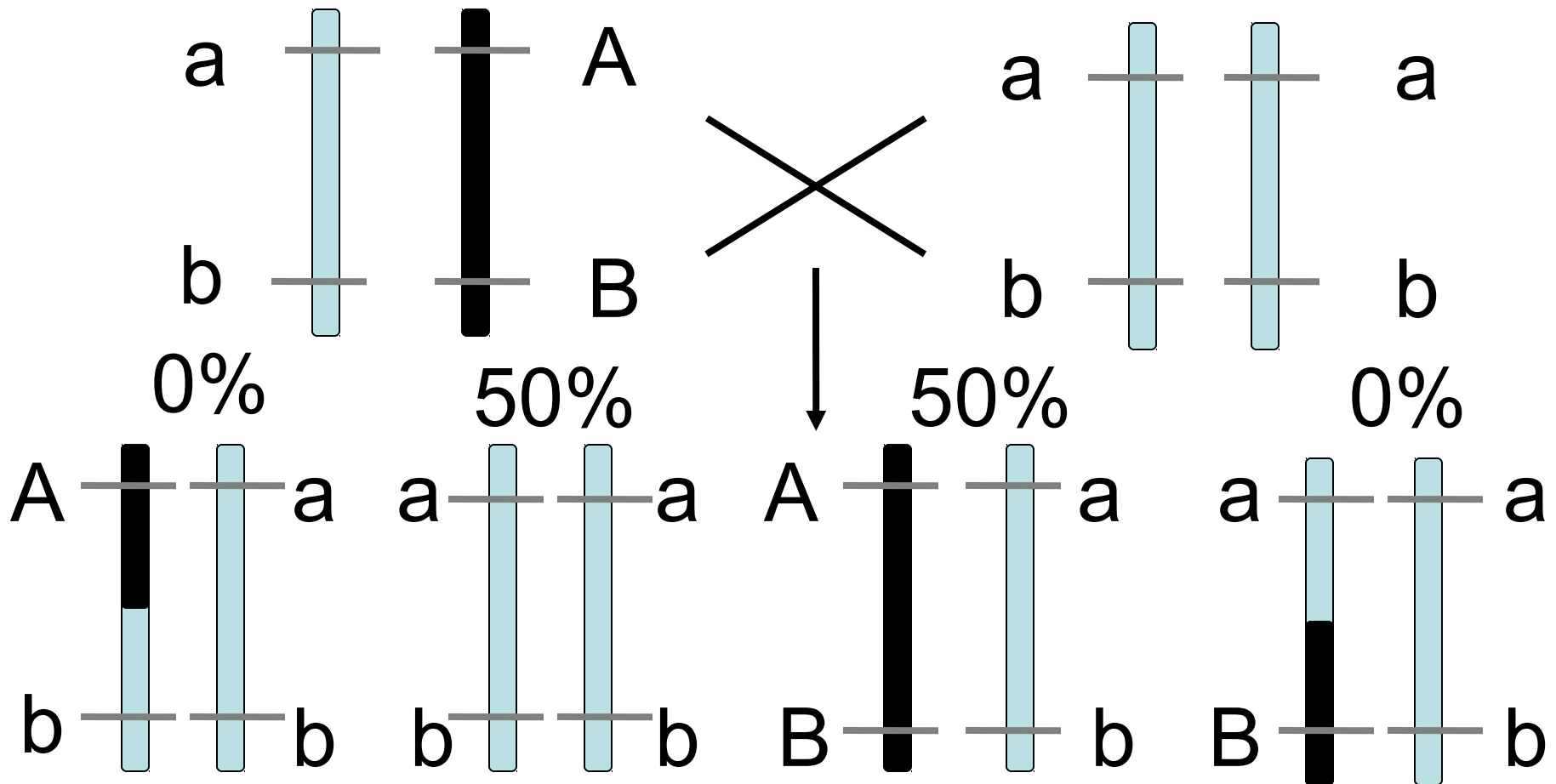
# Recombination– was there recombination?



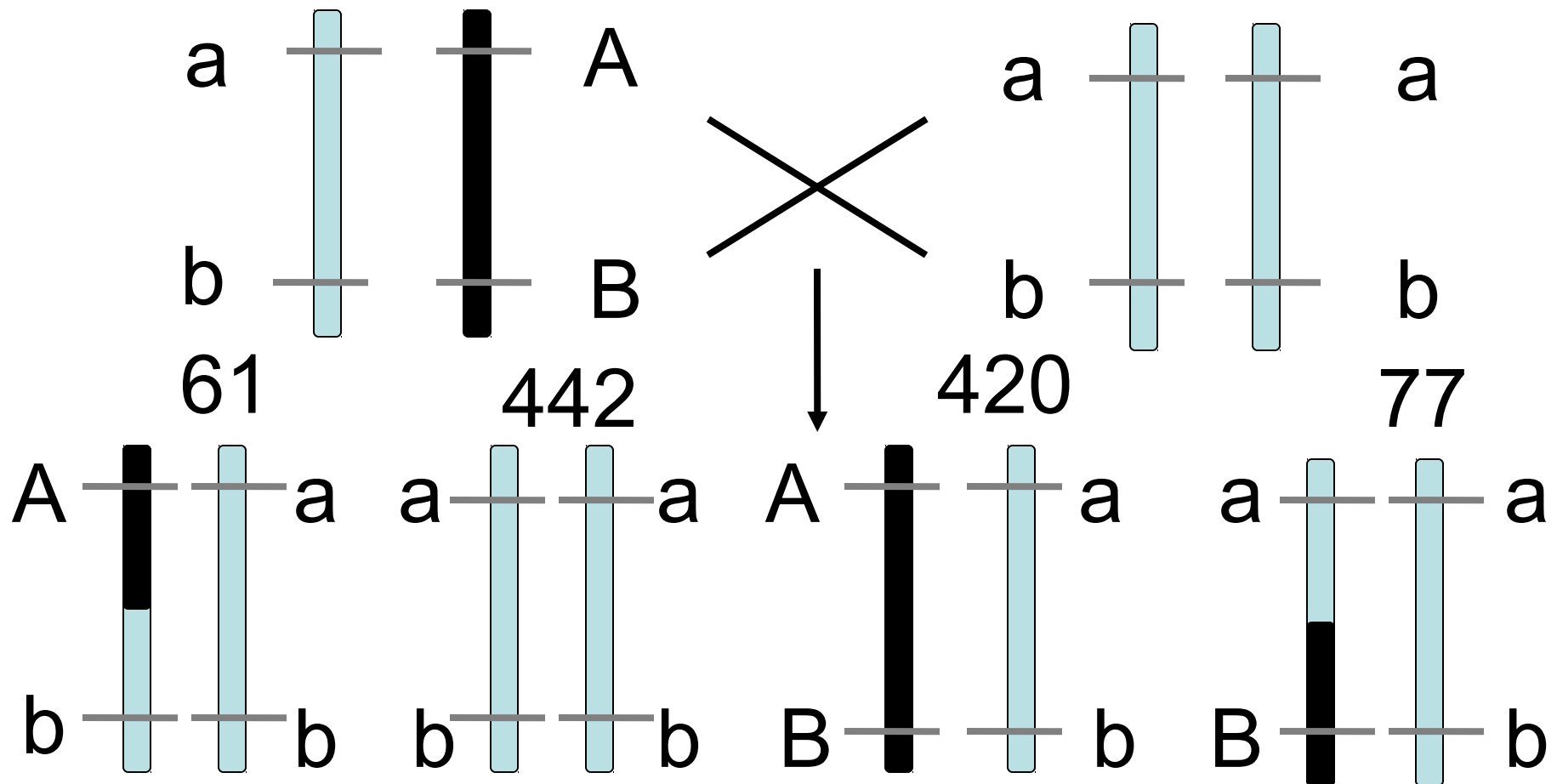
# Independent Assortment



# No recombination



# Recombination Fraction



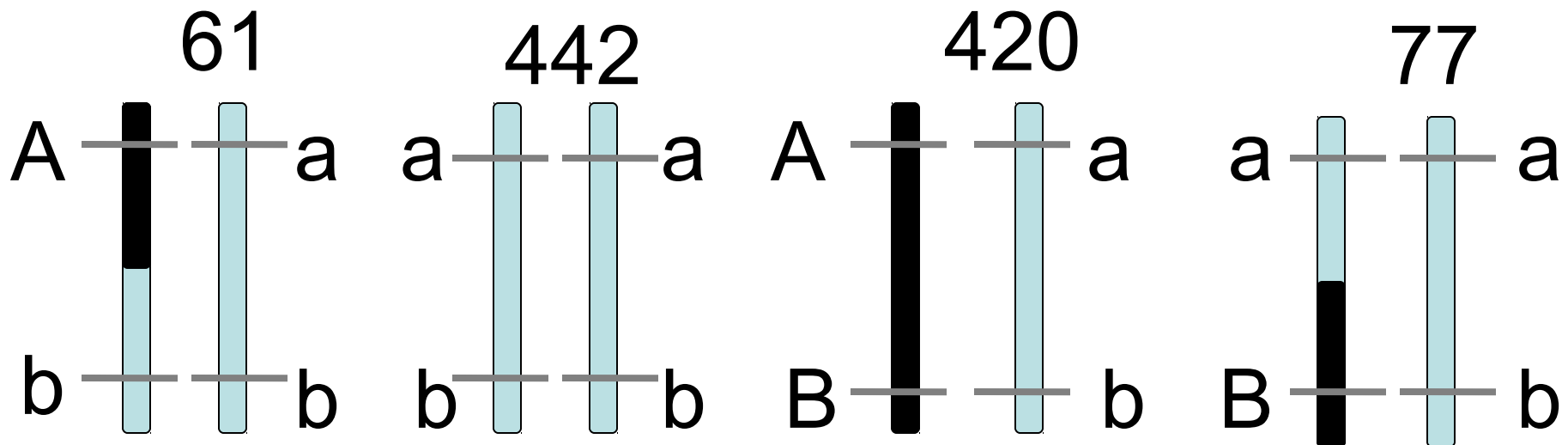
# Recombination Fraction

Recombination Fraction  $\theta$  =

Recombinants / Total =

$$(61+77)/(61+77+442+420)=138/1000$$

= 13.8% < 50%, indicating  
some linkage

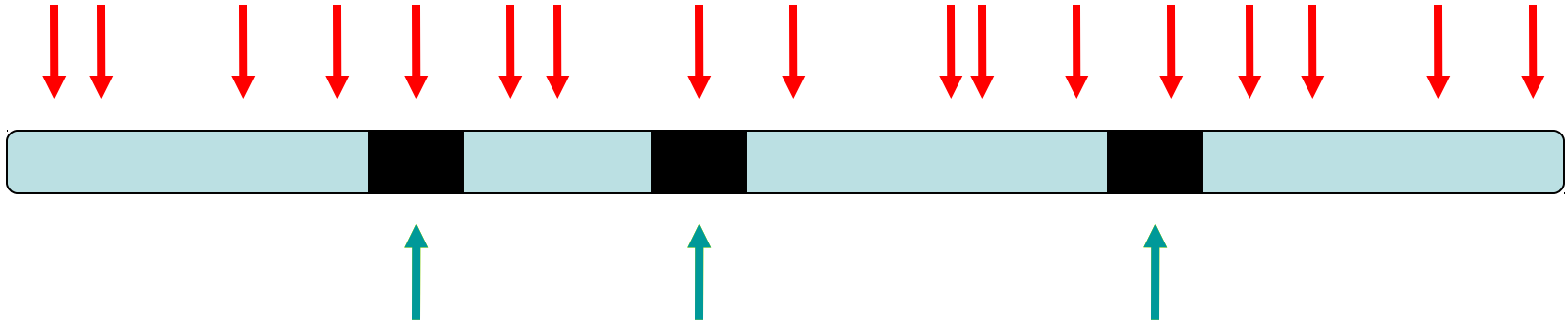


# Human Linkage Analysis

- RFLP Markers for Linkage (1980)
- Huntington's Disease Linkage (1983)
- Cystic Fibrosis Linkage (1985)
- Cystic Fibrosis Gene (1989)
- Huntington's Disease Gene (1993)

# Genome-wide linkage analysis

Genetic Markers



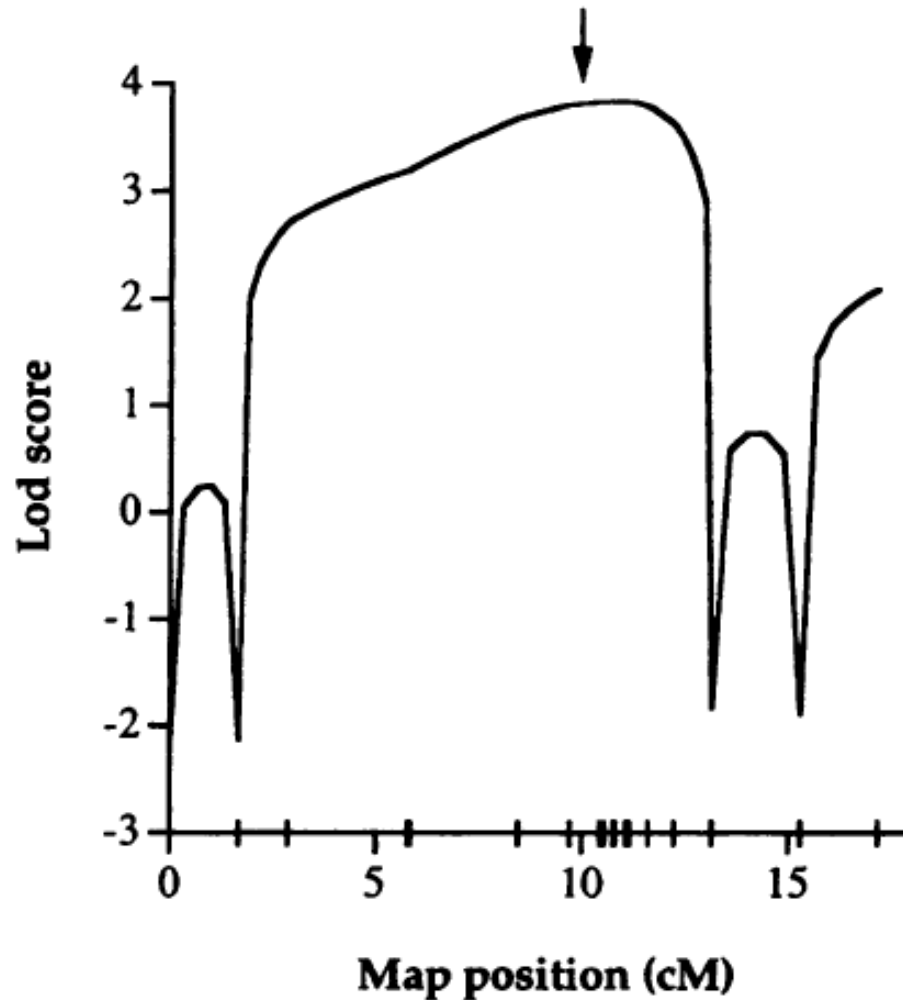
Genes

# Linkage Analysis

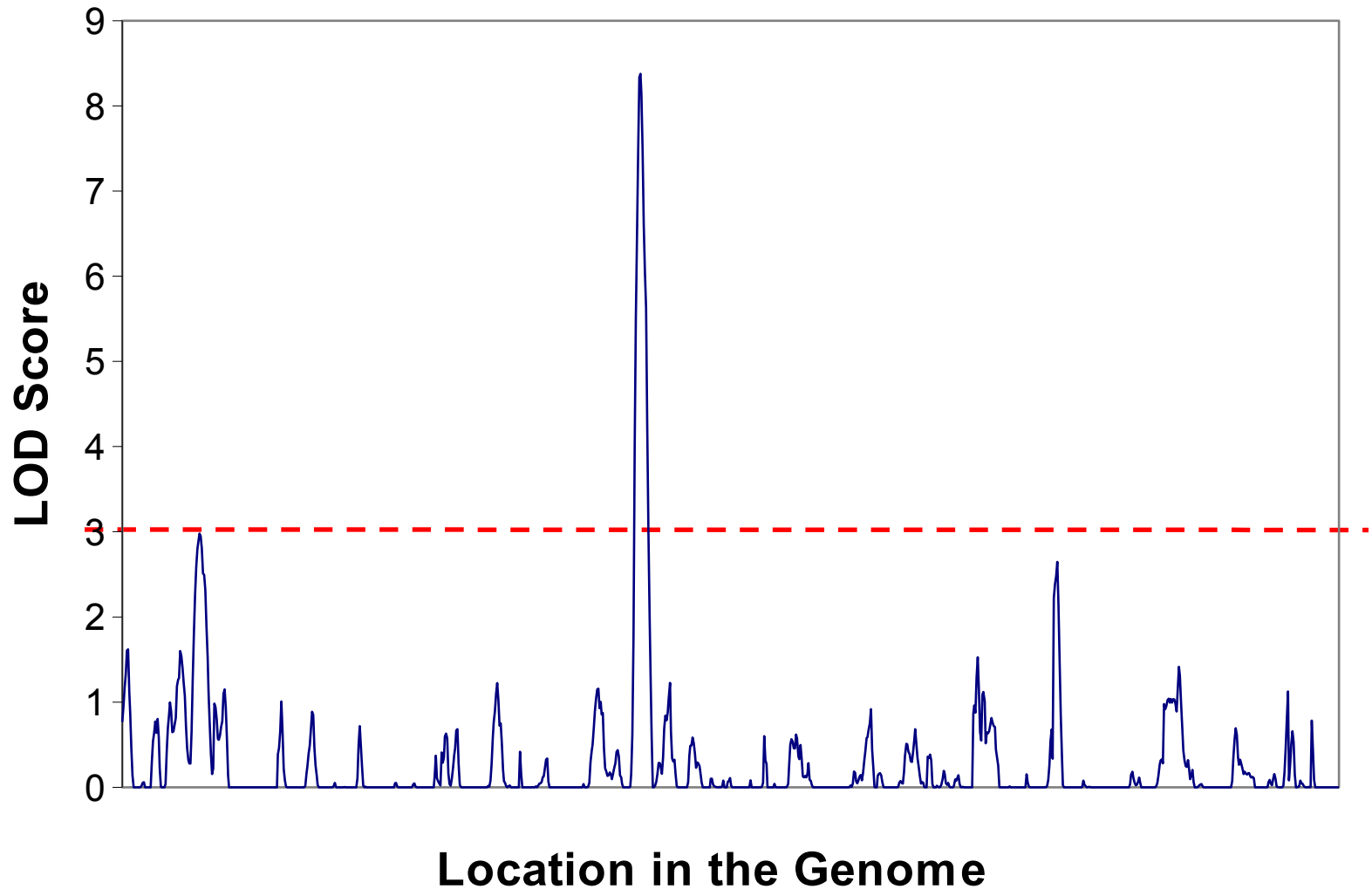
LOD score based on recombination

$$\text{LOD } (\theta) = \log \left( \frac{(\theta)^R (1 - \theta)^{NR}}{(\theta = 1/2)^{R + NR}} \right)$$

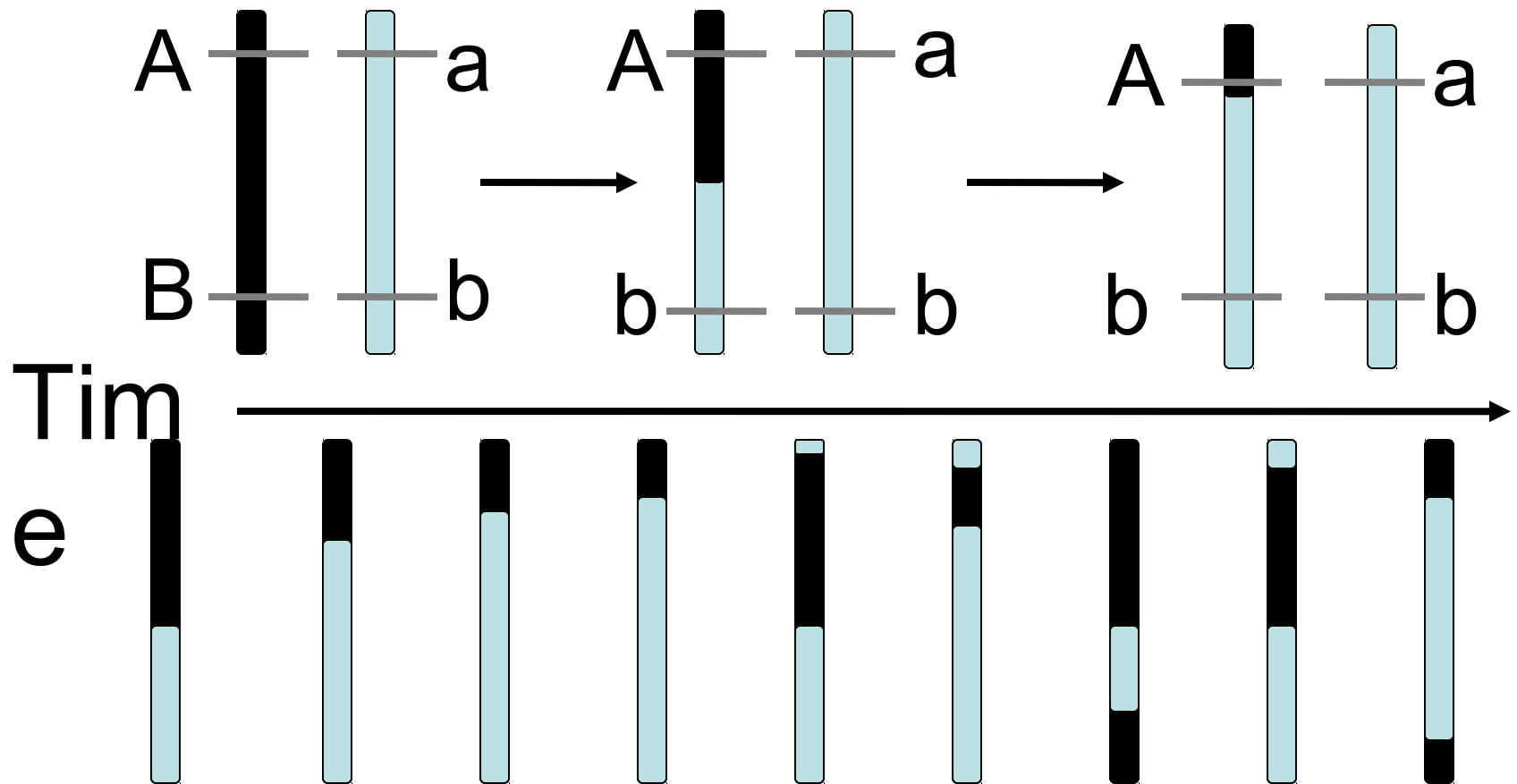
# Multipoint Linkage Analysis



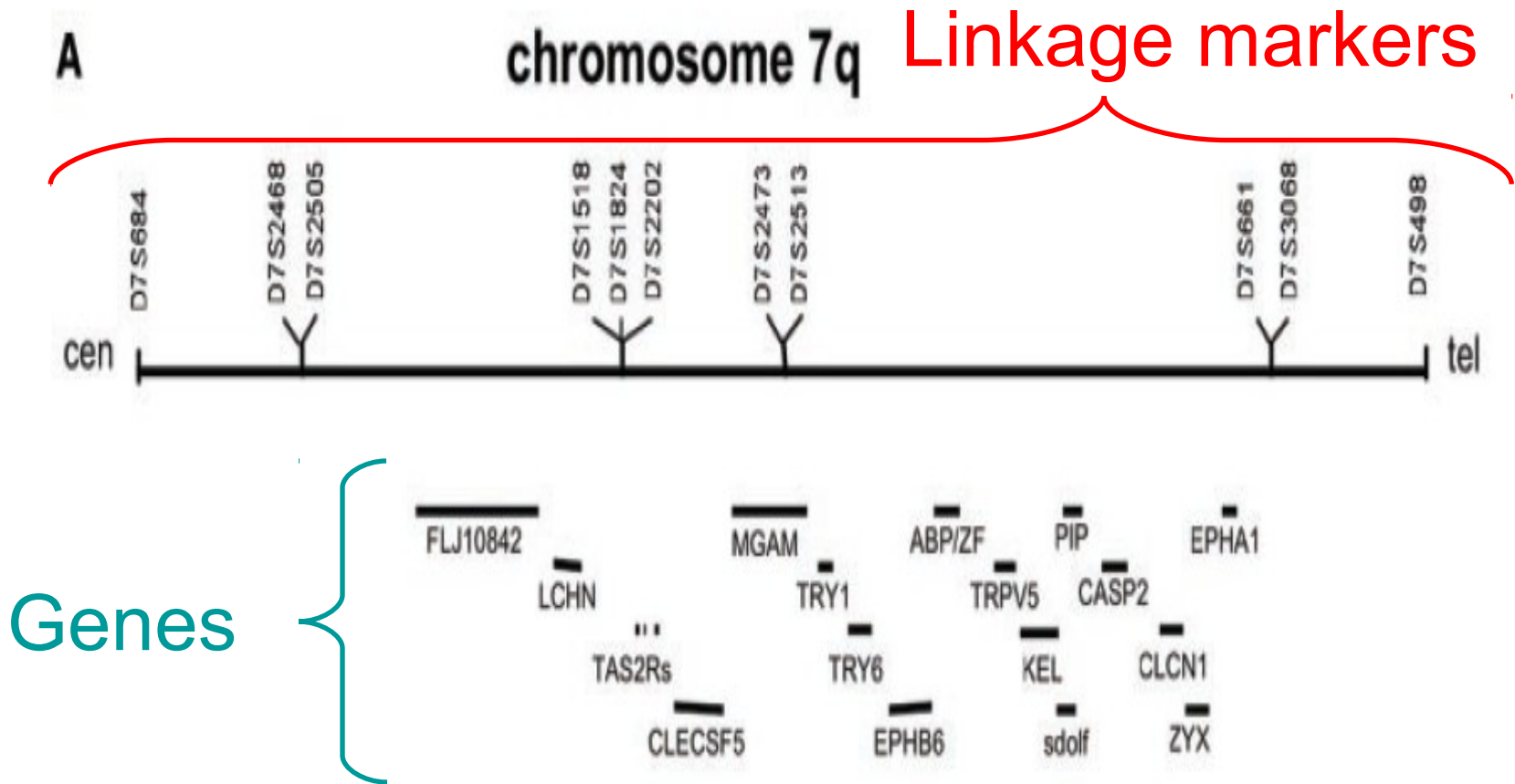
# PTC Linkage Analysis



# Linkage Disequilibrium

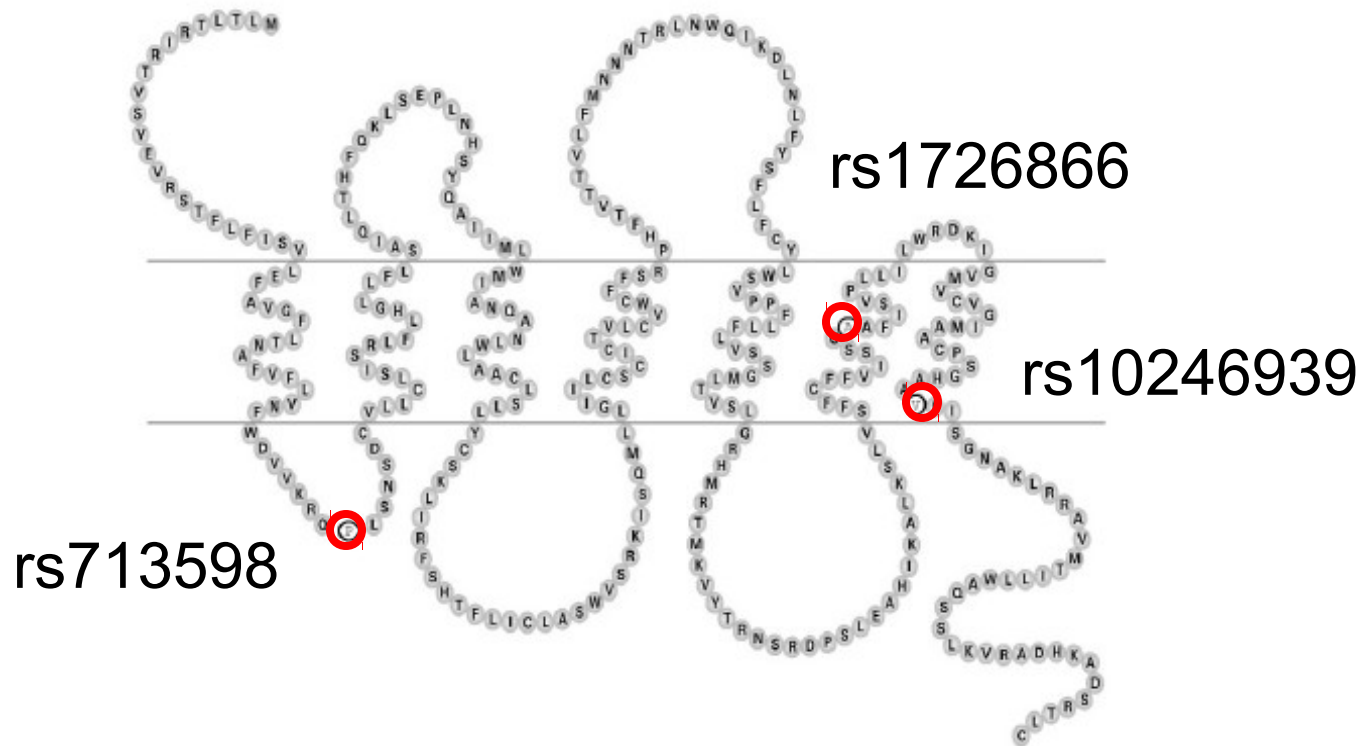


# Fine Mapping



Kim et al. Science 2003

# TAS2R38 Receptor Structure



Kim et al. J Dent Res 2004

# 3 SNPs form 3 Haplotypes

Taster

P

A

V

Non-taster

A

V

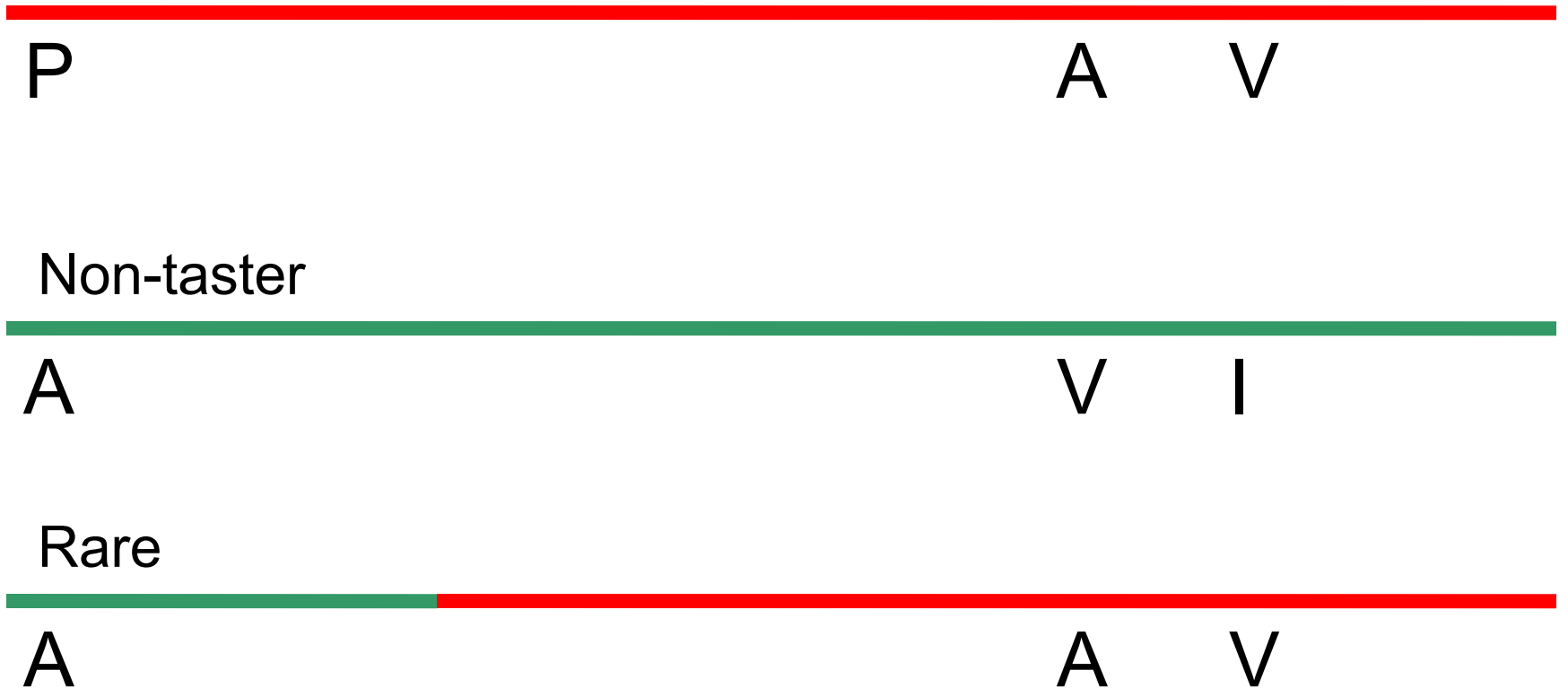
I

Rare

A

A

V



# Predicted Effect of the 3 SNPs

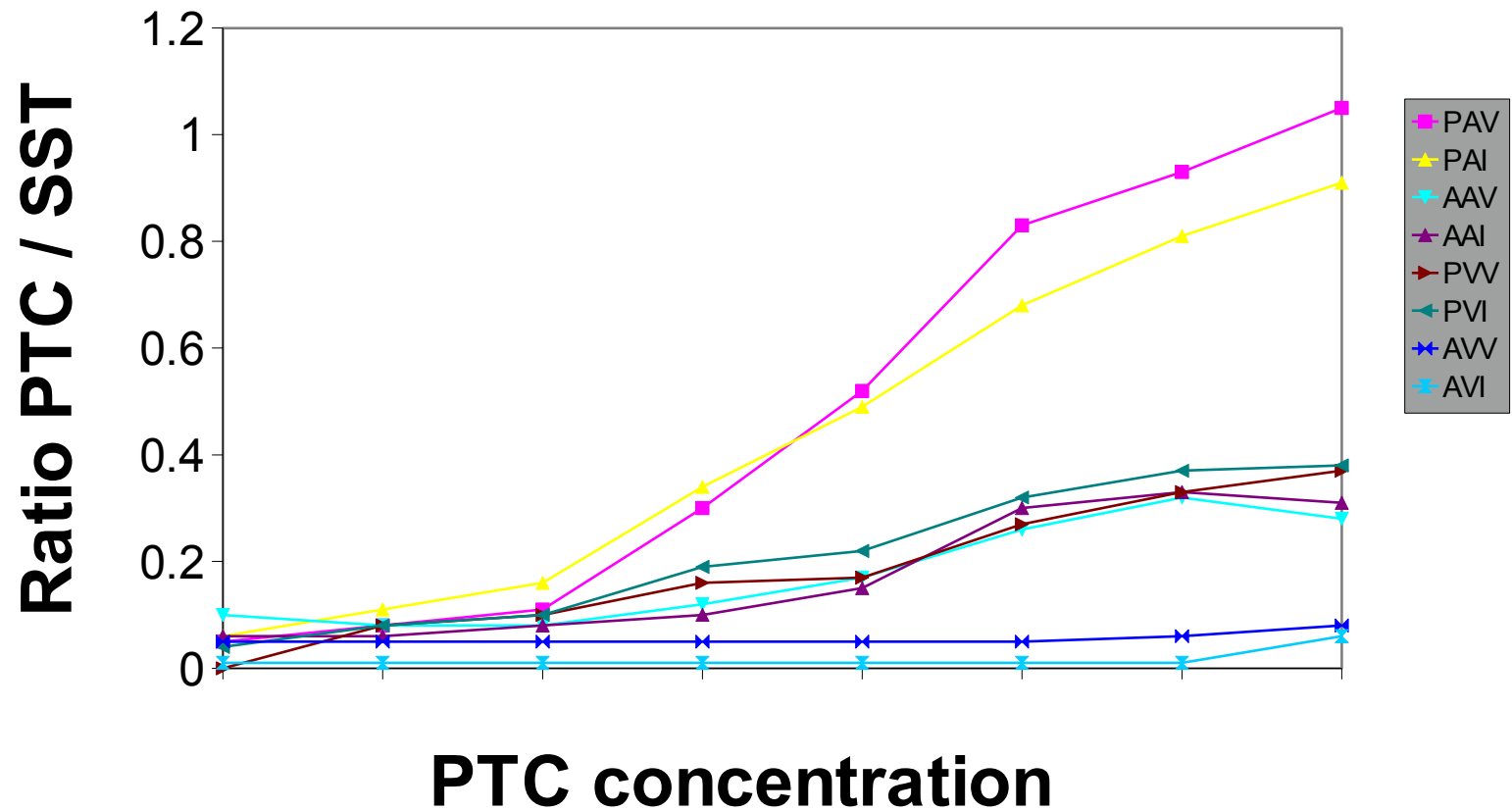
| Amino Acid Substitution | PAM250 |
|-------------------------|--------|
|-------------------------|--------|

|         |   |
|---------|---|
| P --> A | 1 |
|---------|---|

|         |   |
|---------|---|
| A --> V | 0 |
|---------|---|

|         |   |
|---------|---|
| V --> I | 4 |
|---------|---|

# TAS2R38 Haplotype function in vitro



# Outline

- Review last weeks homeworks
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  - (Had just finished HWE game)
  - Population stratification
- Linkage analysis, with PTC testing example
- **Family-based association tests**
  - **Overview**
  - **Trios/TDT**
  - **Discordant sibships**

# Mendelian transmission: Ex

- E.g., parents are Aa, Aa:
  - $P(\text{offspring}=AA \mid \text{Mother}=Aa, \text{Father}=Aa)=?$
  - $P(\text{offspring}=Aa \mid \text{Mother}=Aa, \text{Father}=Aa)=?$
  - $P(\text{offspring}=aa \mid \text{Mother}=Aa, \text{Father}=Aa)=?$

# Mendelian transmission: Ex

- E.g., parents are Aa, Aa:
  - $P(\text{offspring}=AA \mid \text{Mother}=Aa, \text{Father}=Aa)=1/4$
  - $P(\text{offspring}=Aa \mid \text{Mother}=Aa, \text{Father}=Aa)=1/2$
  - $P(\text{offspring}=aa \mid \text{Mother}=Aa, \text{Father}=Aa)=1/4$

| M\F | A  | a  |
|-----|----|----|
| A   | AA | Aa |
| a   | Aa | aa |

Conditioning on  
parents...

# Mendelian transmission: Ex

- E.g., parents are AA, Aa:
  - $P(\text{offspring}=AA \mid \text{Mother}=AA, \text{Father}=Aa)=?$
  - $P(\text{offspring}=Aa \mid \text{Mother}=AA, \text{Father}=Aa)=?$
  - $P(\text{offspring}=aa \mid \text{Mother}=AA, \text{Father}=Aa)=?$

| M\F | A  | a  |
|-----|----|----|
| A   | AA | Aa |
| A   | AA | Aa |

# Mendelian transmission: Ex

- E.g., parents are AA, Aa:
  - $P(\text{offspring}=AA \mid \text{Mother}=AA, \text{Father}=Aa)=1/2$
  - $P(\text{offspring}=Aa \mid \text{Mother}=AA, \text{Father}=Aa)=1/2$
  - $P(\text{offspring}=aa \mid \text{Mother}=AA, \text{Father}=Aa)=0$

| M\F | A  | a  |
|-----|----|----|
| A   | AA | Aa |
| A   | AA | Aa |

# Mendelian transmission: Ex

- E.g., parents are AA, AA:
  - $P(\text{offspring}=AA \mid \text{Mother}=AA, \text{Father}=AA)=?$
  - $P(\text{offspring}=Aa \mid \text{Mother}=AA, \text{Father}=AA)=?$
  - $P(\text{offspring}=aa \mid \text{Mother}=AA, \text{Father}=AA)=?$

| M\F | A  | A  |
|-----|----|----|
| A   | AA | AA |
| A   | AA | AA |

# Mendelian transmission: Ex

- E.g., parents are AA, AA:
  - $P(\text{offspring}=AA \mid \text{Mother}=AA, \text{Father}=AA)=1$
  - $P(\text{offspring}=Aa \mid \text{Mother}=AA, \text{Father}=AA)=0$
  - $P(\text{offspring}=aa \mid \text{Mother}=AA, \text{Father}=AA)=0$

| M\F | A  | A  |
|-----|----|----|
| A   | AA | AA |
| A   | AA | AA |

*Homozygote parents are “non-informative” (no variation in offspring’s conditional genotype distribution)*

# Trios: Transmission Disequilibrium Test (TDT)

- Test based on transmissions from parents to offspring
- Assumptions
  - Parents' and offspring genotypes known
  - dichotomous phenotype (though Q-TDT), only affected offspring
- Count transmissions from heterozygote parents, and compare to expected transmissions
  - Mendel's laws of segregation (previous slides), not control group
  - test for over/under-transmission of alleles in cases (intuition...)
- Conditional test
  - offspring affection status
  - Parental genotypes (conditions out allele frequencies, which is what case-control is based on testing)

# Trios: Transmission Disequilibrium Test (TDT)

|                             |   | Non-transmitted parental allele |   |
|-----------------------------|---|---------------------------------|---|
|                             |   | A                               | a |
| Transmitted parental allele | A | w                               | x |
|                             | a | y                               | z |

- w AA parents (transmit one A, do not transmit other A)
- z aa parents (transmit one a, do not transmit other a)
- x Aa parents that transmit A, do not transmit a
- y Aa parents that transmit a, do not transmit A

# Possible Parental Configurations

- **AA-AA, AA-Aa, AA-aa, Aa-AA, Aa-Aa, Aa-aa, aa-AA, aa-Aa, aa-aa**
  - (Ones not bolded are symmetric for what we will do next, e.g., AA-Aa == Aa-AA)
  - Six possible configurations

# Both parents homozygous

|                             |   | Non-transmitted parental allele |   | AA - AA |
|-----------------------------|---|---------------------------------|---|---------|
|                             |   | A                               | a |         |
| Transmitted parental allele | A | 2                               | 0 | AA      |
|                             | a | 0                               | 0 |         |

- Offspring genotype is deterministic, no variation, not informative!

# Both parents homozygous

|                             |   | Non-transmitted parental allele |   | aa - aa |
|-----------------------------|---|---------------------------------|---|---------|
|                             |   | A                               | a |         |
| Transmitted parental allele | A | 0                               | 0 | aa      |
|                             | a | 0                               | 2 |         |

- Offspring genotype is deterministic, no variation, not informative!

# Both parents homozygous

|                             |   | Non-transmitted parental allele |   | AA - aa |
|-----------------------------|---|---------------------------------|---|---------|
|                             |   | A                               | a |         |
| Transmitted parental allele | A | 1                               | 0 | Aa      |
|                             | a | 0                               | 1 |         |

- Offspring genotype is deterministic, no variation, not informative!

# One parent heterozygous

|                             |   | Non-transmitted parental allele |   | AA-Aa  |      |  |
|-----------------------------|---|---------------------------------|---|--------|------|--|
|                             |   | A                               | a |        |      |  |
| Transmitted parental allele | A | 1                               | 1 | AA, Aa |      |  |
|                             | a | 0                               | 0 | .5 .5  | ← Pr |  |

|                             |   | Non-transmitted parental allele |   |
|-----------------------------|---|---------------------------------|---|
|                             |   | A                               | a |
| Transmitted parental allele | A | 1                               | 0 |
|                             | a | 1                               | 0 |

- Variation from one parent

# One parent heterozygous

|                             |   | Non-transmitted parental allele |   | Aa - aa |      |  |
|-----------------------------|---|---------------------------------|---|---------|------|--|
|                             |   | A                               | a |         |      |  |
| Transmitted parental allele | A | 0                               | 1 | Aa, aa  |      |  |
|                             | a | 0                               | 1 | .5 .5   | ← Pr |  |

|                             |   | Non-transmitted parental allele |   |
|-----------------------------|---|---------------------------------|---|
|                             |   | A                               | a |
| Transmitted parental allele | A | 0                               | 0 |
|                             | a | 1                               | 1 |

- Variation from one parent

# Both parents heterozygous

|                             |   |                                 |   |            |         |
|-----------------------------|---|---------------------------------|---|------------|---------|
|                             |   | Non-transmitted parental allele |   | Aa - Aa    |         |
|                             |   | A                               | a |            |         |
| Transmitted parental allele | A | 0                               | 2 | AA, Aa, aa |         |
|                             | a | 0                               | 0 | .5         | .5 ← Pr |

|                             |   |                                 |   |                             |   |                                 |   |
|-----------------------------|---|---------------------------------|---|-----------------------------|---|---------------------------------|---|
|                             |   | Non-transmitted parental allele |   |                             |   | Non-transmitted parental allele |   |
|                             |   | A                               | a |                             |   | A                               | a |
| Transmitted parental allele | A | 0                               | 1 | Transmitted parental allele | A | 0                               | 0 |
|                             | a | 1                               | 0 |                             | a | 2                               | 1 |

- Variation from both parents

# Trios: Transmission Disequilibrium Test (TDT)

|                             |   | Non-transmitted parental allele |   |
|-----------------------------|---|---------------------------------|---|
| Transmitted parental allele | A | w                               | x |
|                             | a | y                               | z |

- w AA parents (transmit one A, do not transmit other A)
- z aa parents (transmit one a, do not transmit other a)
- x Aa parents that transmit A, do not transmit a
- y Aa parents that transmit a, do not transmit A

# Transmission Disequilibrium Test (TDT)

|                             |   |                                 |   |
|-----------------------------|---|---------------------------------|---|
|                             |   | Non-transmitted parental allele |   |
|                             |   | A                               | a |
| Transmitted parental allele | A | w                               | x |
|                             | a | y                               | z |

- No variation in w or z (recall homozygous parents non informative)
- $(x-y)^2/(x+y) \sim \chi_1^2$ ; it's just special case of McNemar's test
- Think of it as testing are there an excess of the A allele in the affected offspring than would happen by Mendel's laws?

# Transmission Disequilibrium Test (TDT)

|                             |   | Non-transmitted parental allele |    | Insulin Dependent Diabetes Mellitus (IDDM) |
|-----------------------------|---|---------------------------------|----|--------------------------------------------|
|                             |   | A                               | a  |                                            |
| Transmitted parental allele | A | ?                               | 78 |                                            |
|                             | a | 46                              | ?  |                                            |

- Example from the text: 94 families, 78 parents transmit allele A, 46 transmit allele a
- $(78-46)^2/(78+46)=8.26$ , p-value=0.004

# Limitations of TDT

- Limitations
  - Only affected offspring
  - Only dichotomous phenotypes
  - Bi-allelic markers
  - Additive genetic model
  - No missing parents
  - Can't do multiple markers, multiple phenotypes
- Extensions exist, e.g., FBAT, ...(*next slide*)...

# Discordant sibships

- Conditional logistic regression
  - $P(Y_1=1|Y_1+Y_2=1, g_1, g_2, \dots)$
  - Matching each sib together, conditions on the fact that *they have discordant phenotypes*
  - Standard model for disease as in logistic regression, just matching based on family strata
- You will go through an example in the homework

# Summary

- Family-based studies can be robust to population substructure (based on Mendelian transmissions, not population allele frequencies)
- Robust to HWE failure
- Powerful for very rare, highly penetrant traits